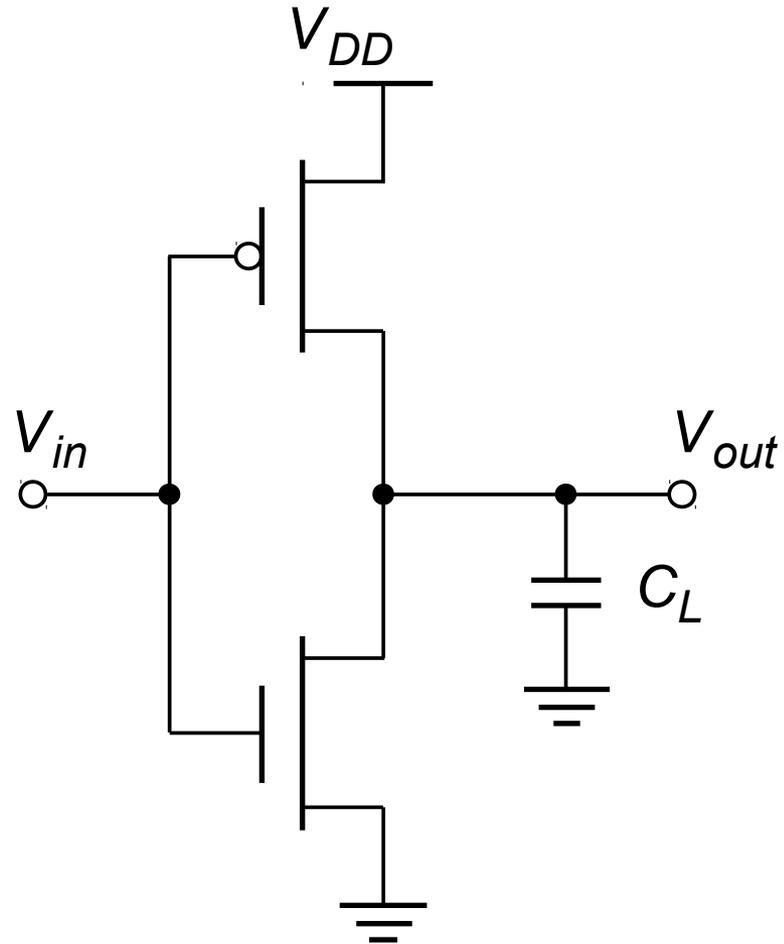


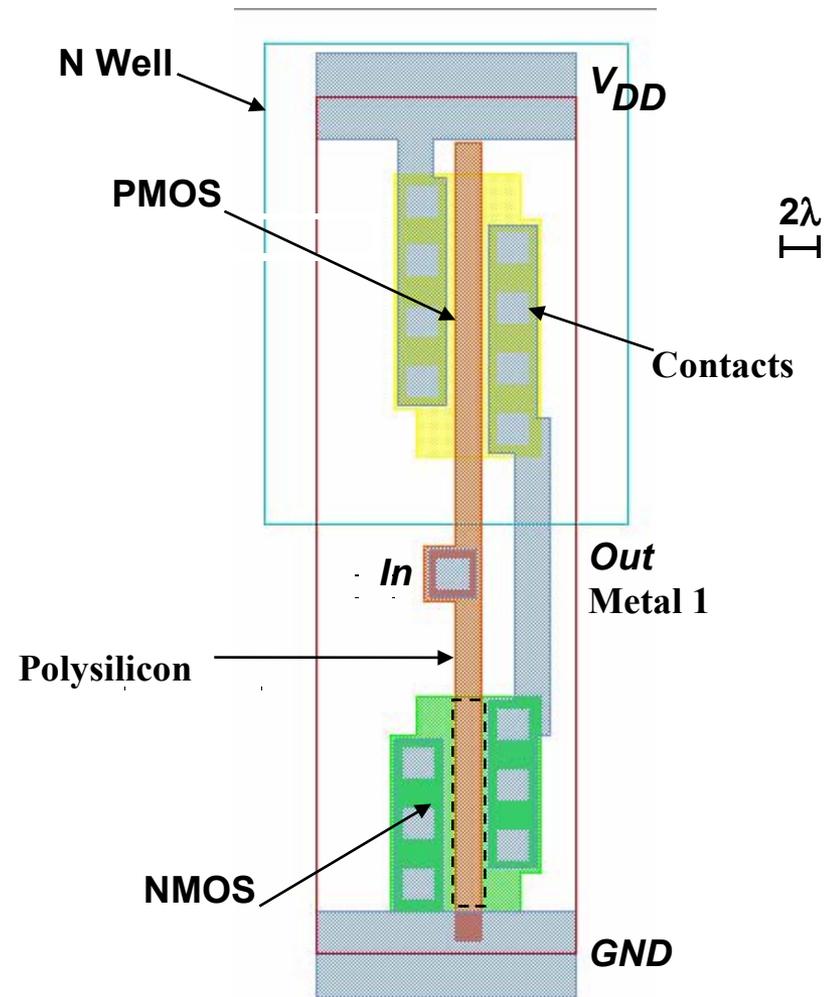
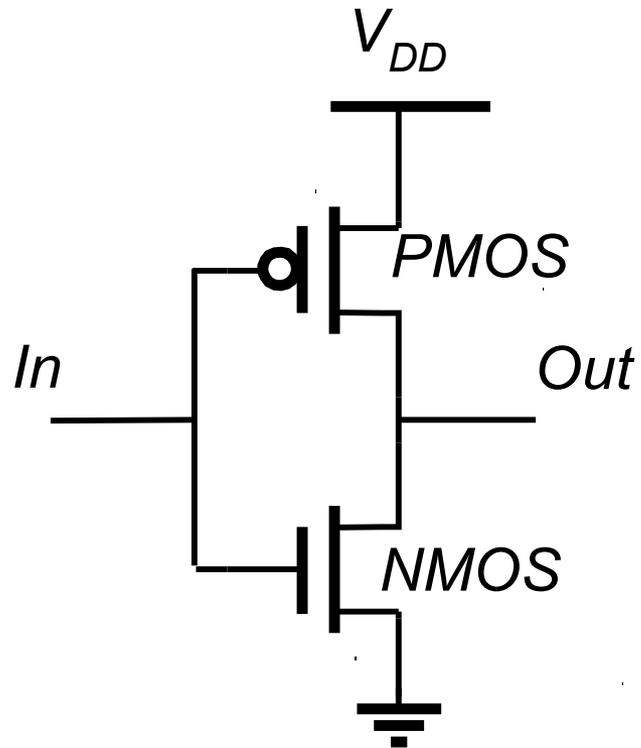
Inversor

Adaptado de
Digital Integrated Circuits
Jan M. Rabaey
Anantha Chandrakasan
Borivoje Nikolic

Inversor CMOS

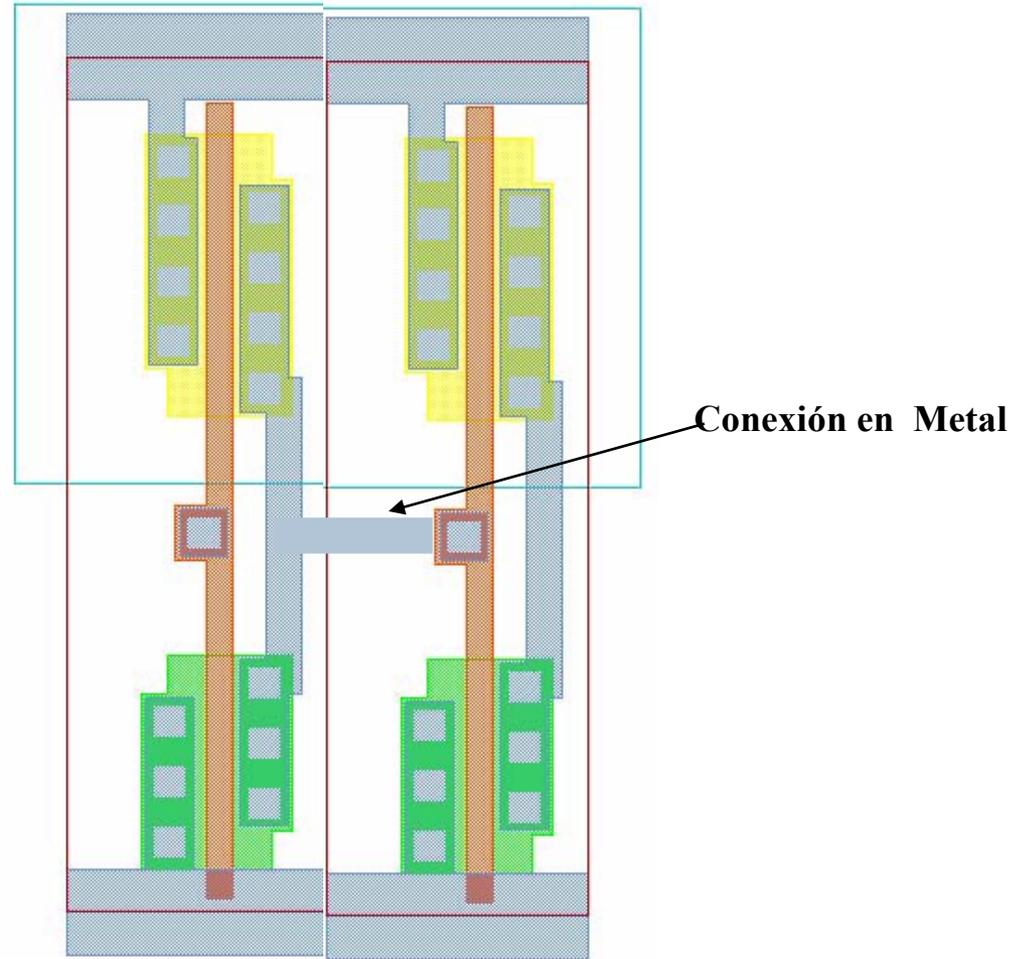
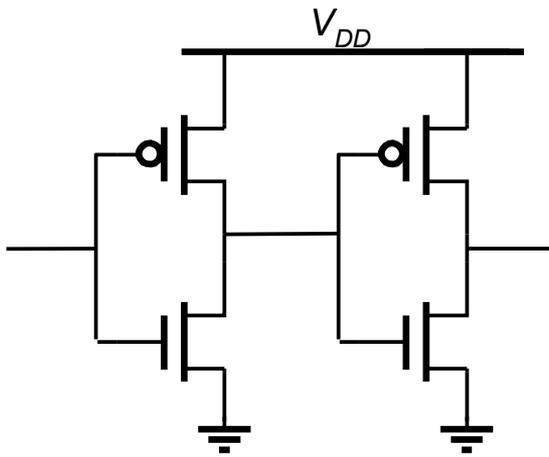


Inversor CMOS

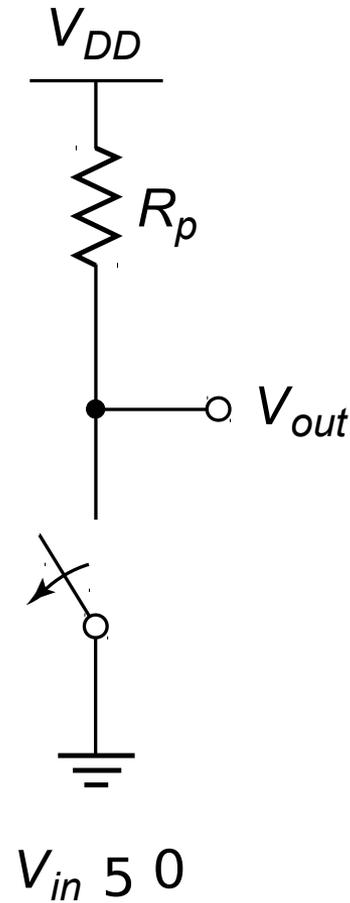
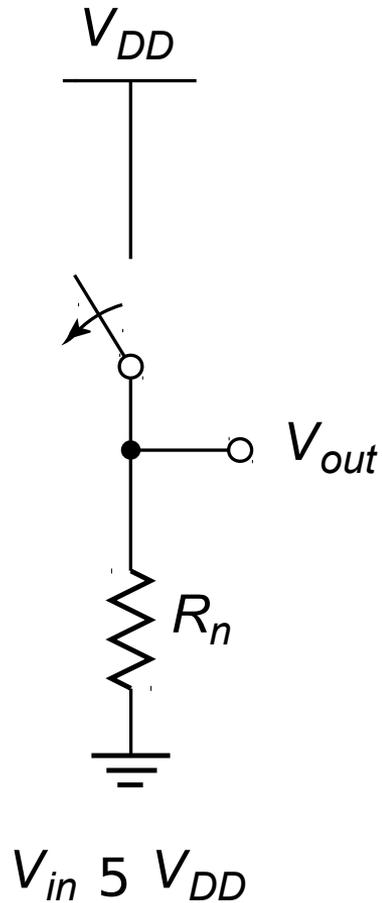


Dos inversores.

Estructura regular.

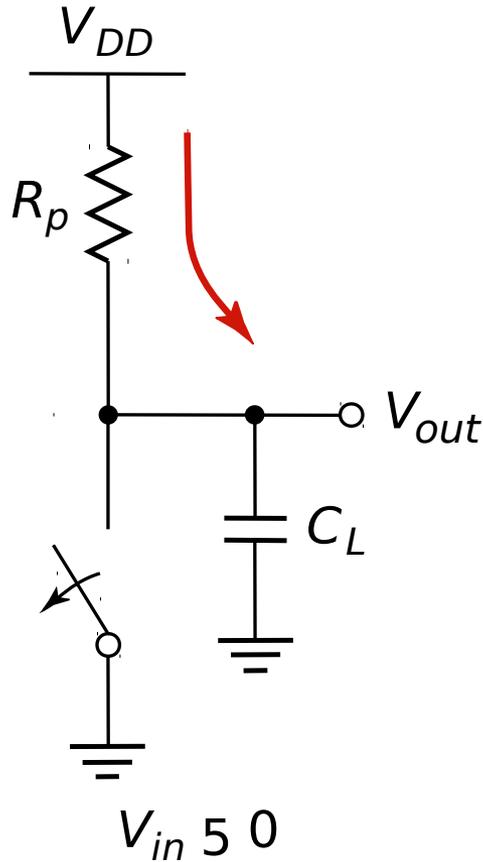


Análisis de primer orden para el caso estático.

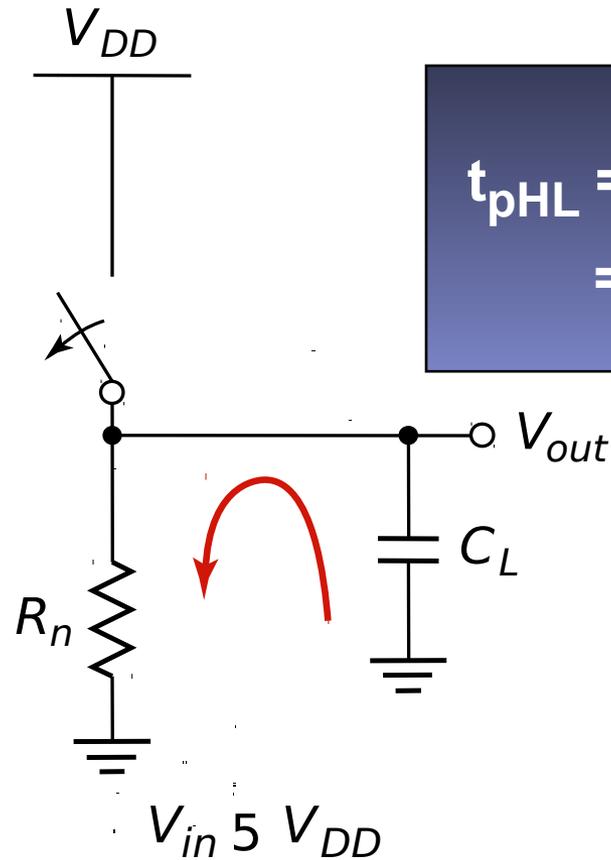


$$\begin{aligned} V_{OL} &= 0 \\ V_{OH} &= V_{DD} \\ V_M &= f(R_n, R_p) \end{aligned}$$

Análisis de primer orden para el caso estático.



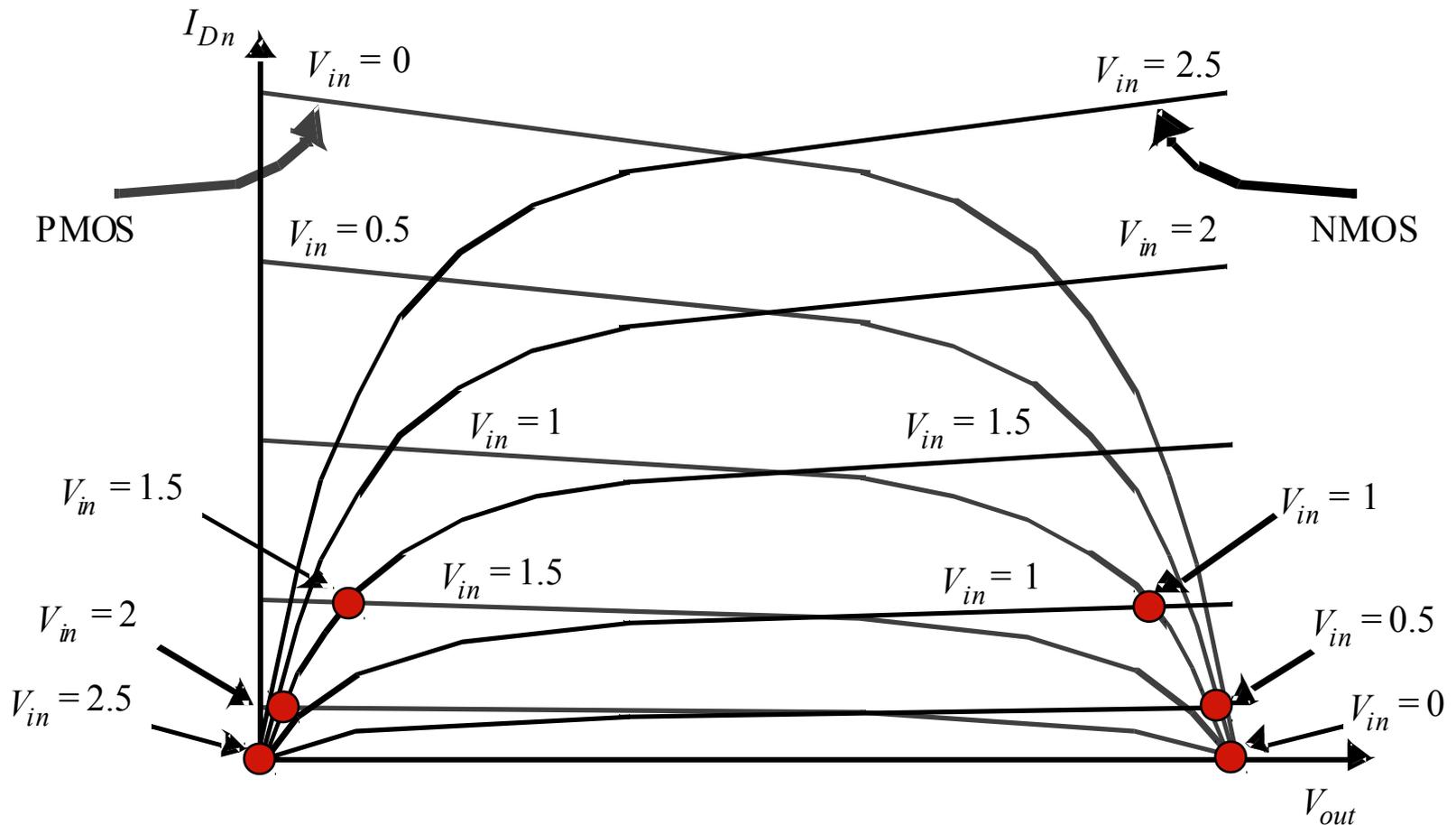
(a) Low-to-high



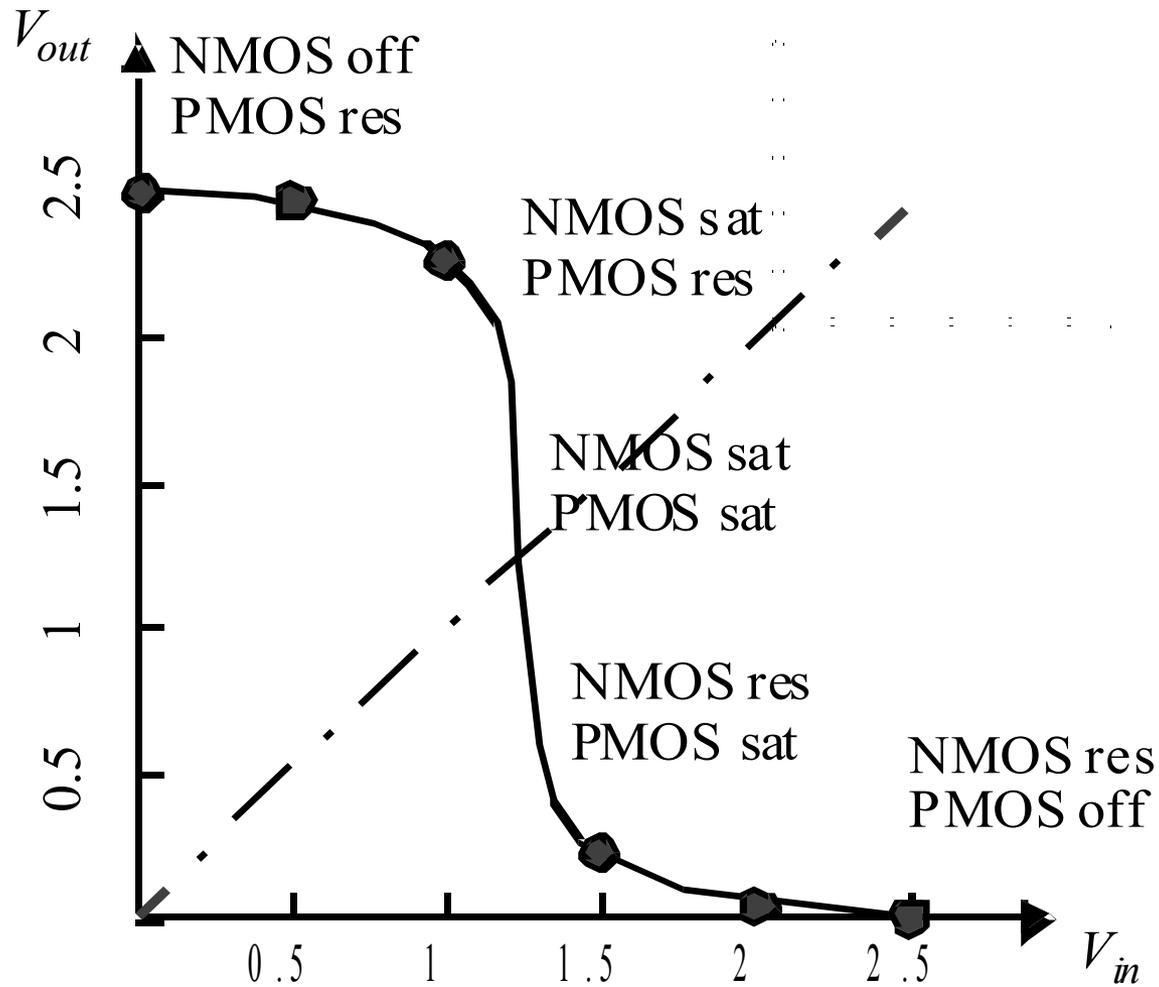
(b) High-to-low

$$t_{pHL} = f(R_{on} \cdot C_L) \\ = 0.69 R_{on} C_L$$

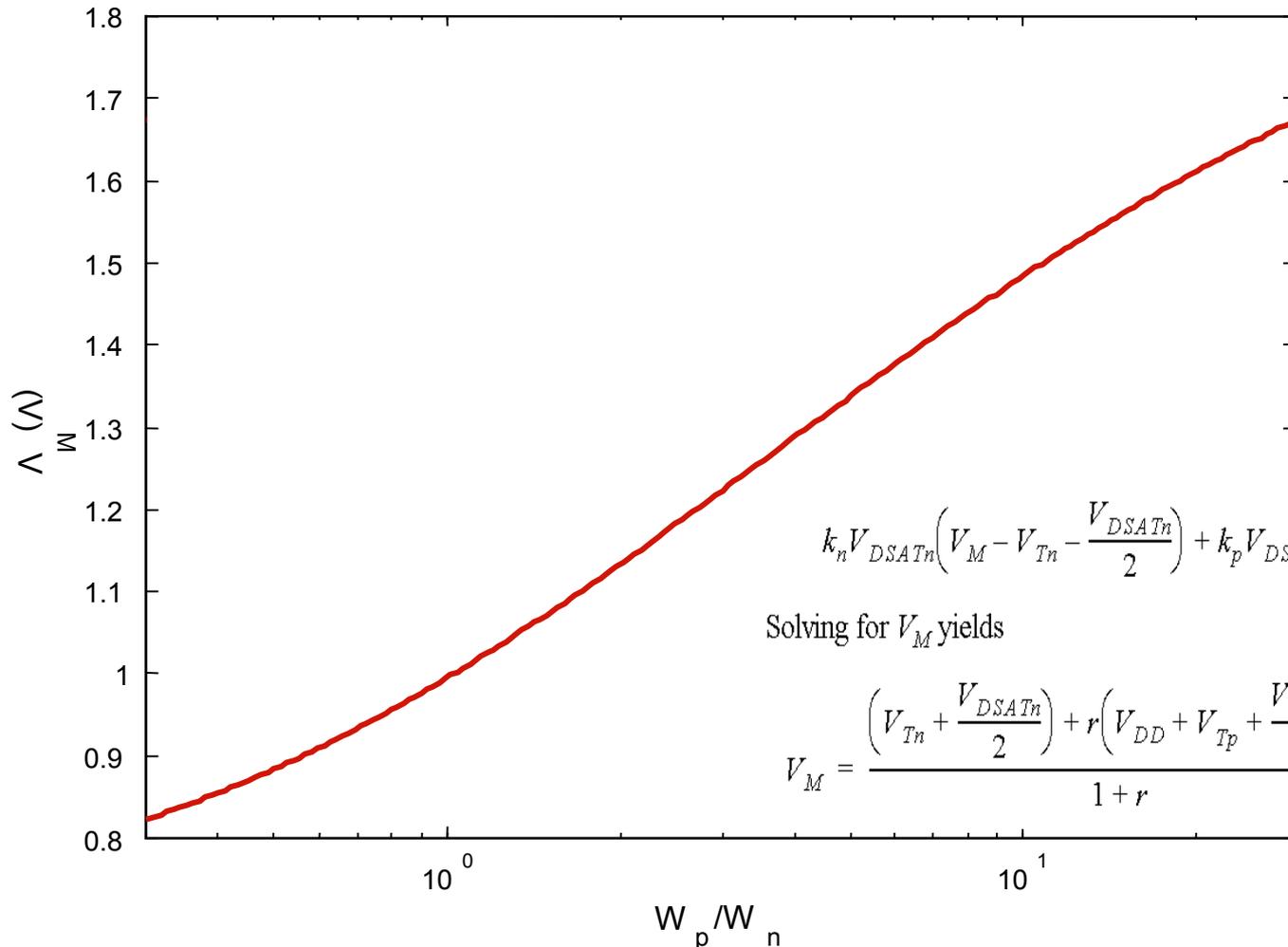
Características estáticas del inversor CMOS.



Curvas de transferencia.



Umbral de switching vs ratio de nMOS y pMOS

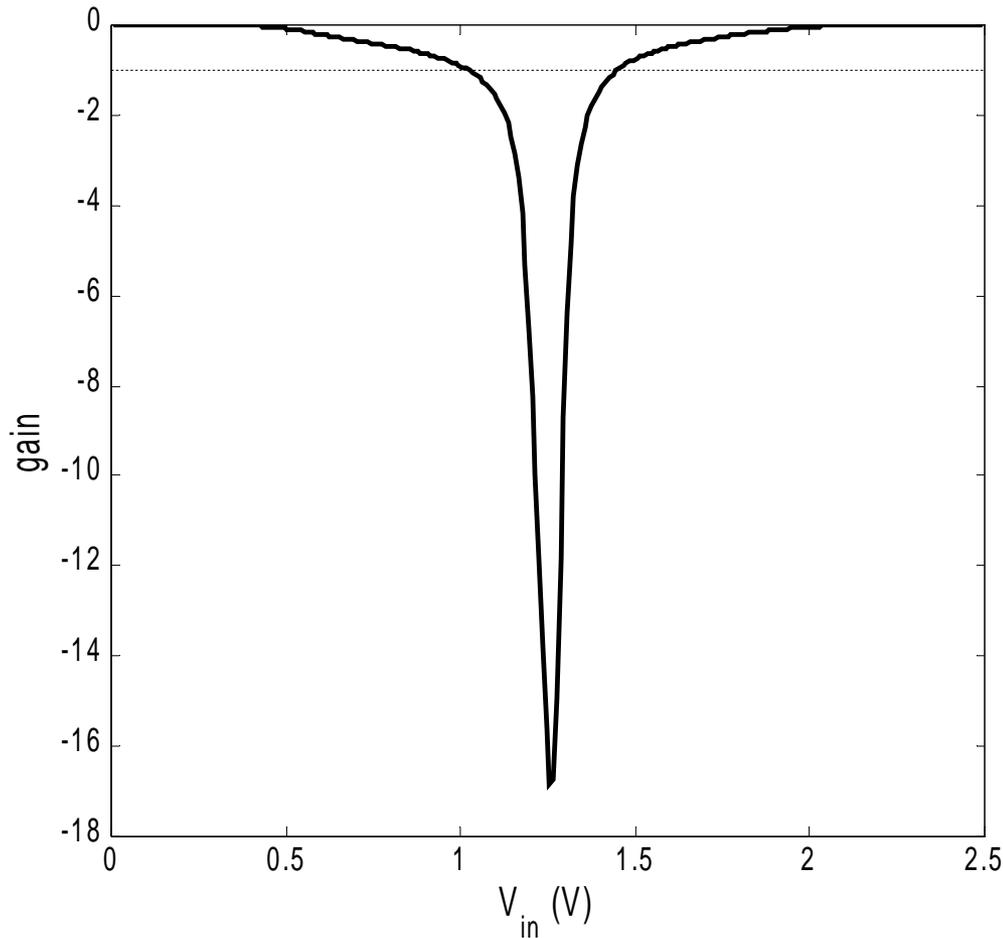


$$k_n V_{DSATn} \left(V_M - V_{Tn} - \frac{V_{DSATn}}{2} \right) + k_p V_{DSATp} \left(V_M - V_{DD} - V_{Tp} - \frac{V_{DSATp}}{2} \right) = 0$$

Solving for V_M yields

$$V_M = \frac{\left(V_{Tn} + \frac{V_{DSATn}}{2} \right) + r \left(V_{DD} + V_{Tp} + \frac{V_{DSATp}}{2} \right)}{1 + r} \quad \text{with } r = \frac{k_p V_{DSATp}}{k_n V_{DSATn}} = \frac{v_{satp} W_p}{v_{satn} W_n}$$

Ganancia del inversor.



$$g = -\frac{1}{I_D(V_M)} \frac{k_n V_{DSATn} + k_p V_{DSATp}}{\lambda_n - \lambda_p}$$
$$\approx \frac{1+r}{(V_M - V_{Tn} - V_{DSATn}/2)(\lambda_n - \lambda_p)}$$

¿Cuál es el mínimo Vdd posible?

Características...

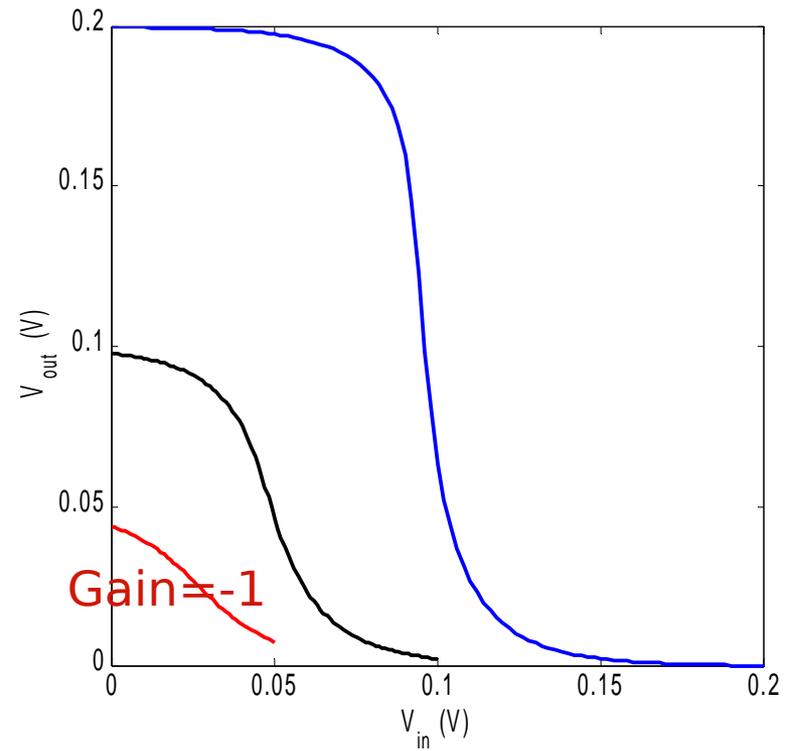
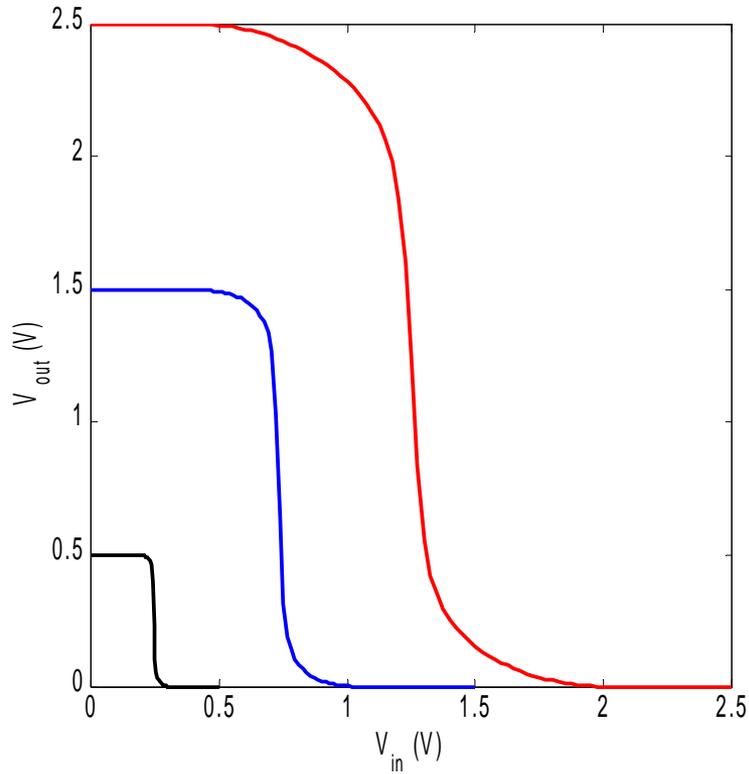
¿El funcionamiento depende del ratio n/p ?

¿Valores alto y bajo?

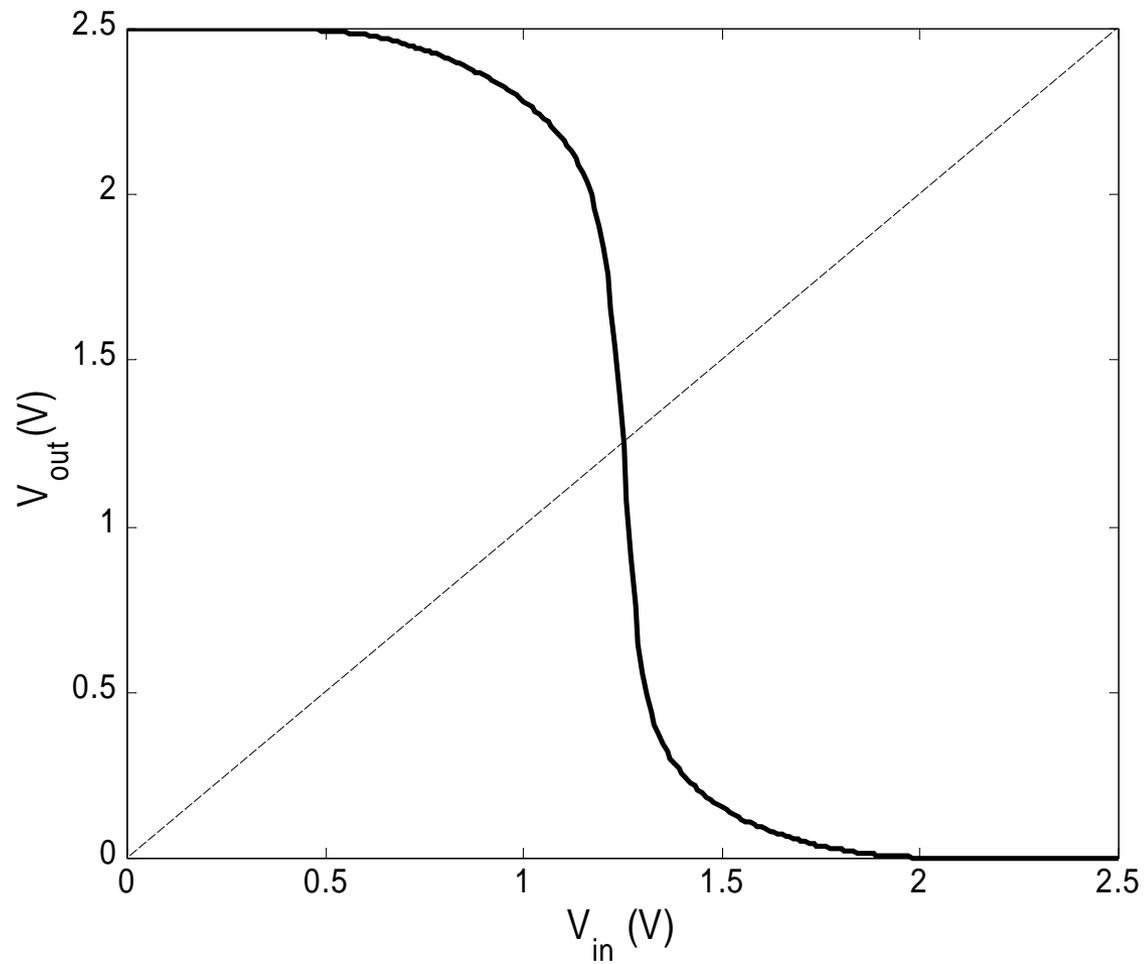
¿Consumos estático y dinámico?

¿Resistencia de entrada?

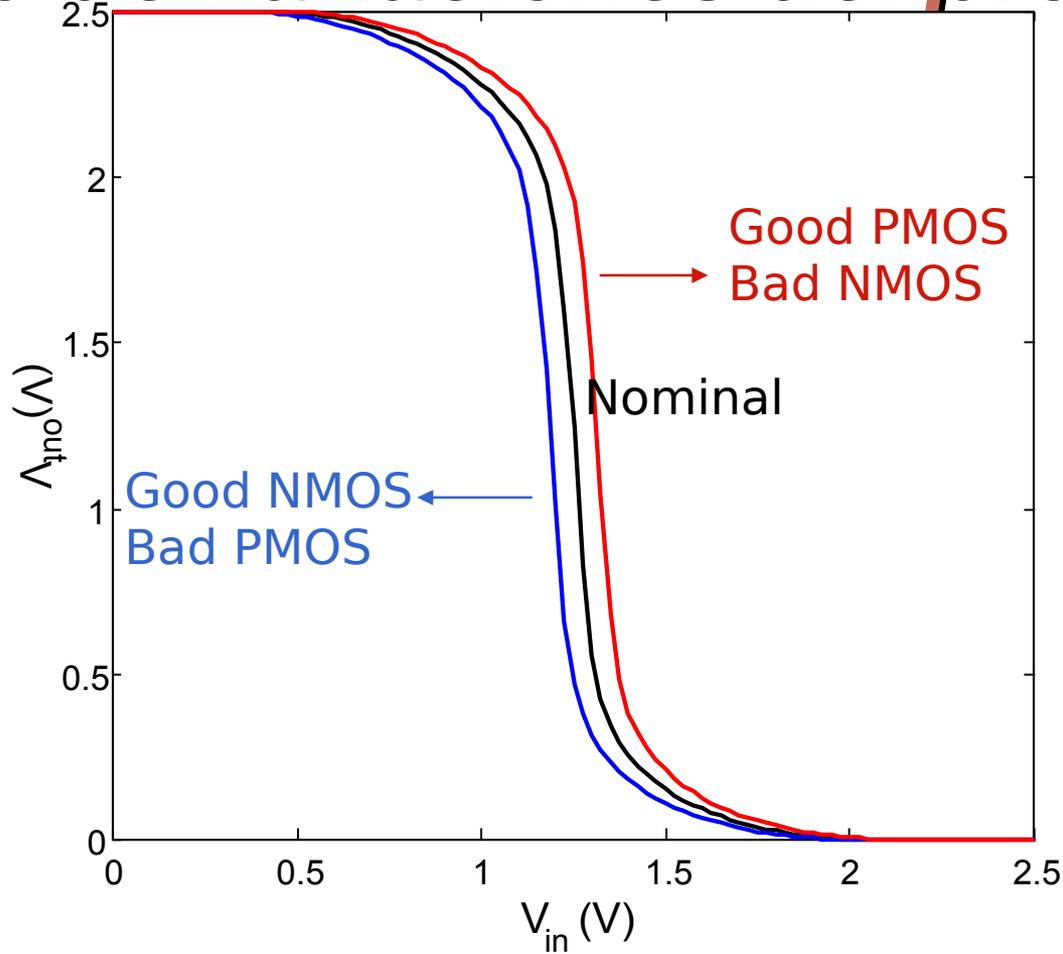
Ganancia vs Vdd

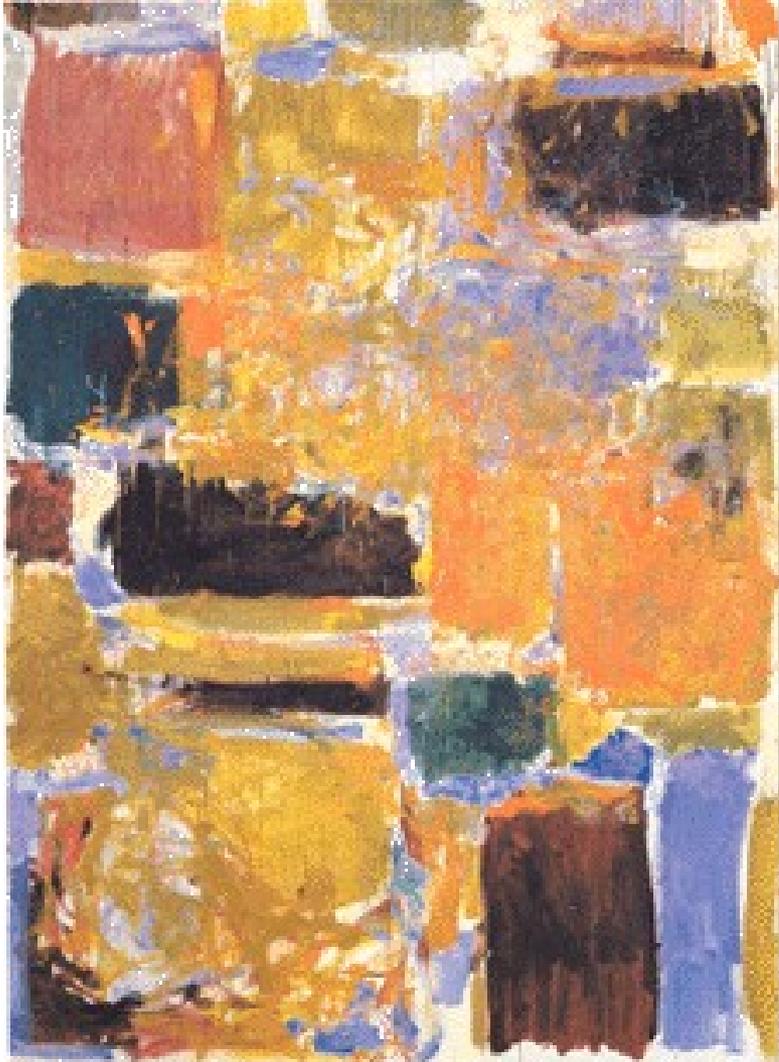


Simulated VTC



Impacto de variaciones del proceso

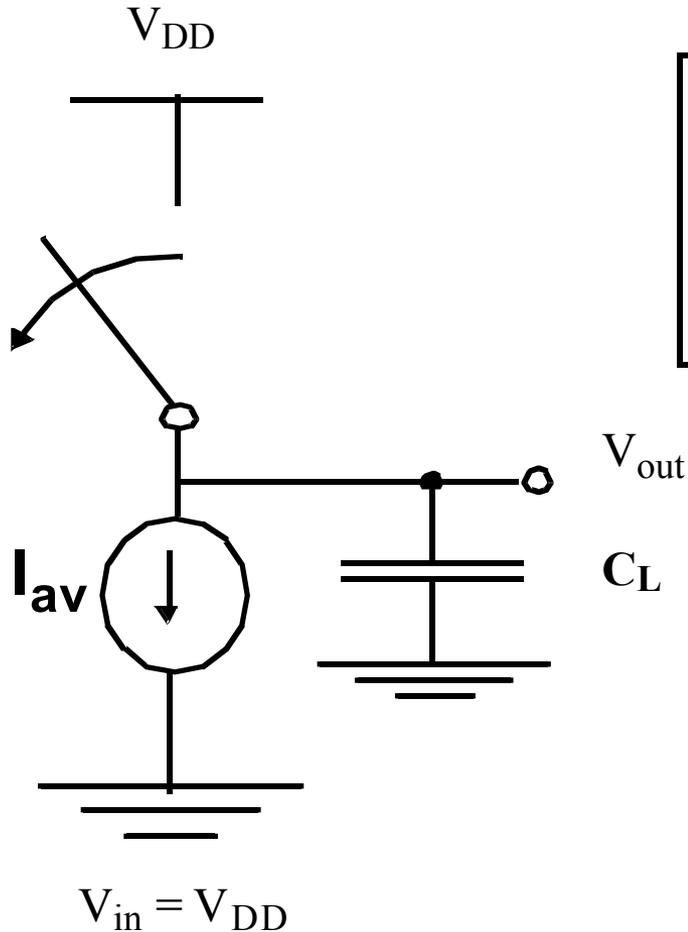




Propagation delay

CMOS Inverter Propagation Delay Approach

1

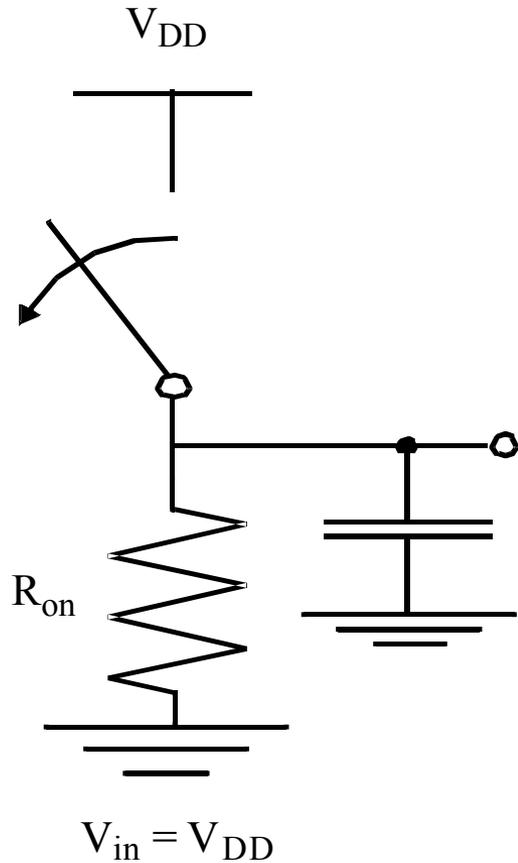


$$t_{pHL} = \frac{C_L V_{swing}/2}{I_{av}}$$

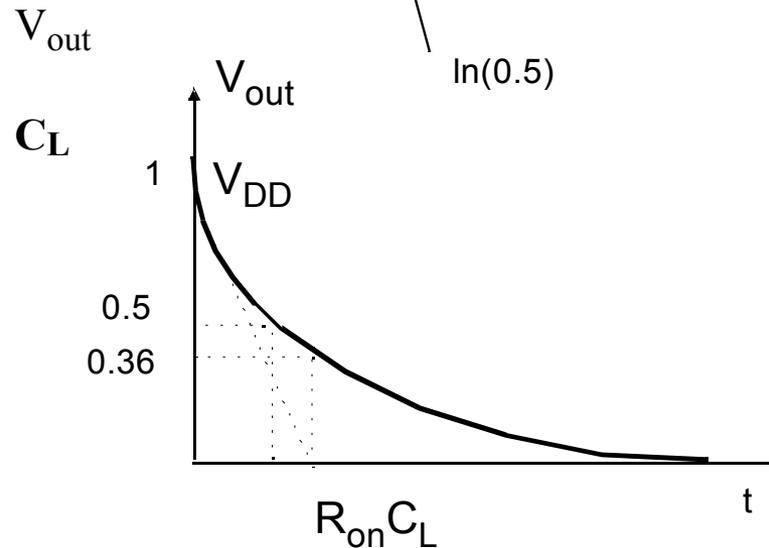
$$\sim \frac{C_L}{k_n V_{DD}}$$

CMOS Inverter Propagation Delay Approach

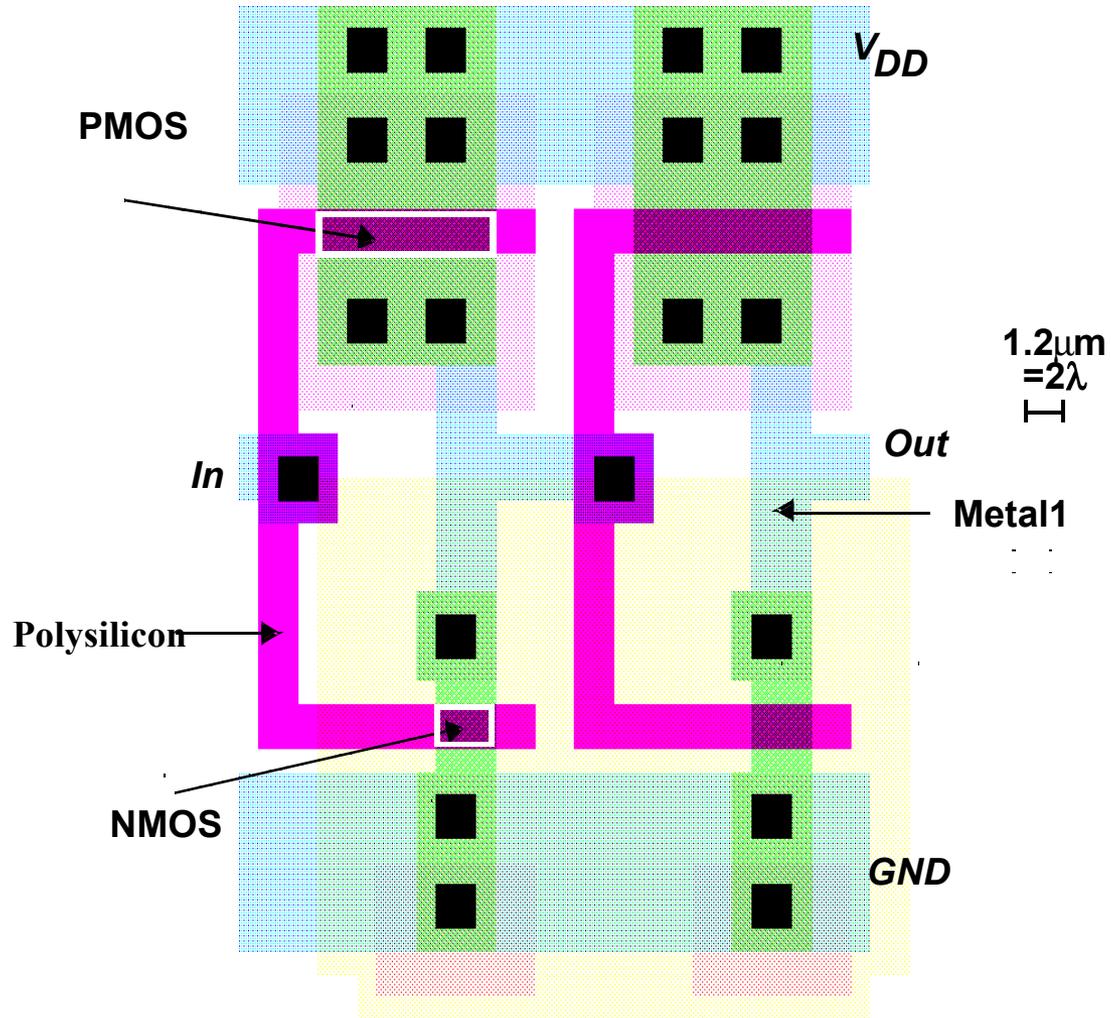
2



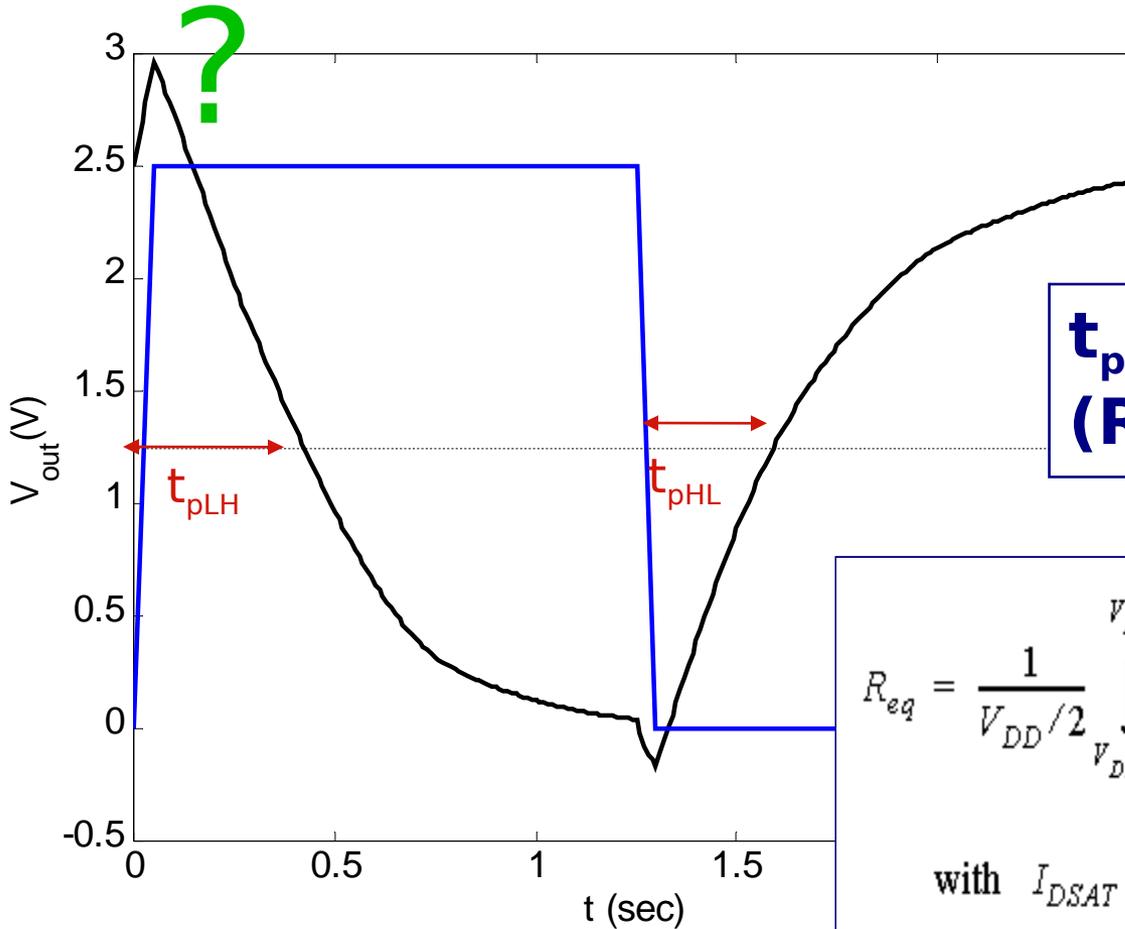
$$t_{pHL} = f(R_{on} \cdot C_L)$$
$$= 0.69 R_{on} C_L$$



Capacidades de carga.



Respuesta temporal



$$t_p = 0.69 C_L (R_{eqn} + R_{eqp}) / 2$$

$$R_{eq} = \frac{1}{V_{DD}/2} \int_{V_{DD}/2}^{V_{DD}} \frac{V}{I_{DSAT}(1 + \lambda V)} dV \approx \frac{3}{4} \frac{V_{DD}}{I_{DSAT}} \left(1 - \frac{7}{9} \lambda V_{DD} \right)$$

with $I_{DSAT} = k' \frac{W}{L} \left((V_{DD} - V_T) V_{DSAT} - \frac{V_{DSAT}^2}{2} \right)$

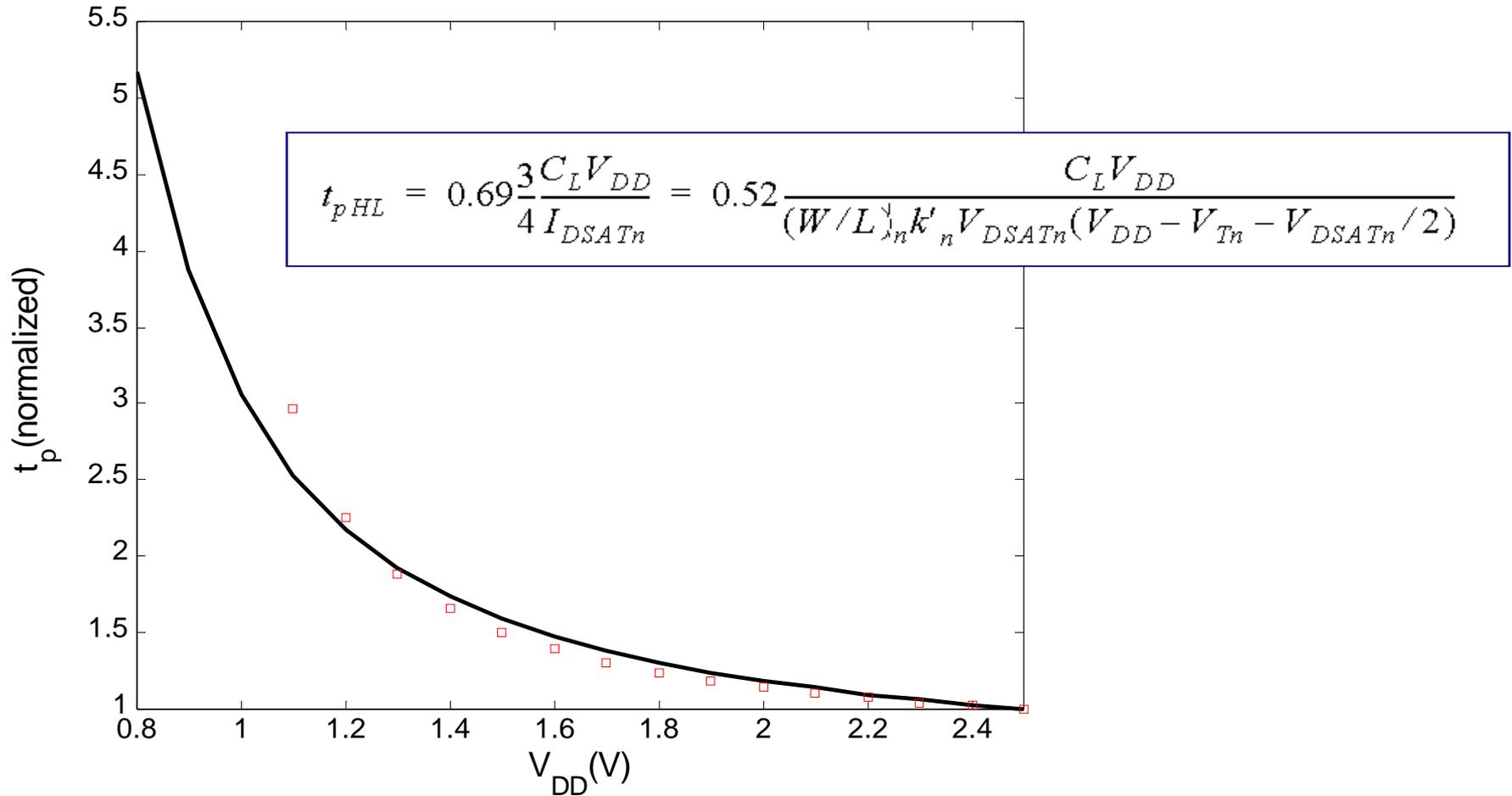
Diseño para mayor performance

¿Cómo mejorar la velocidad?

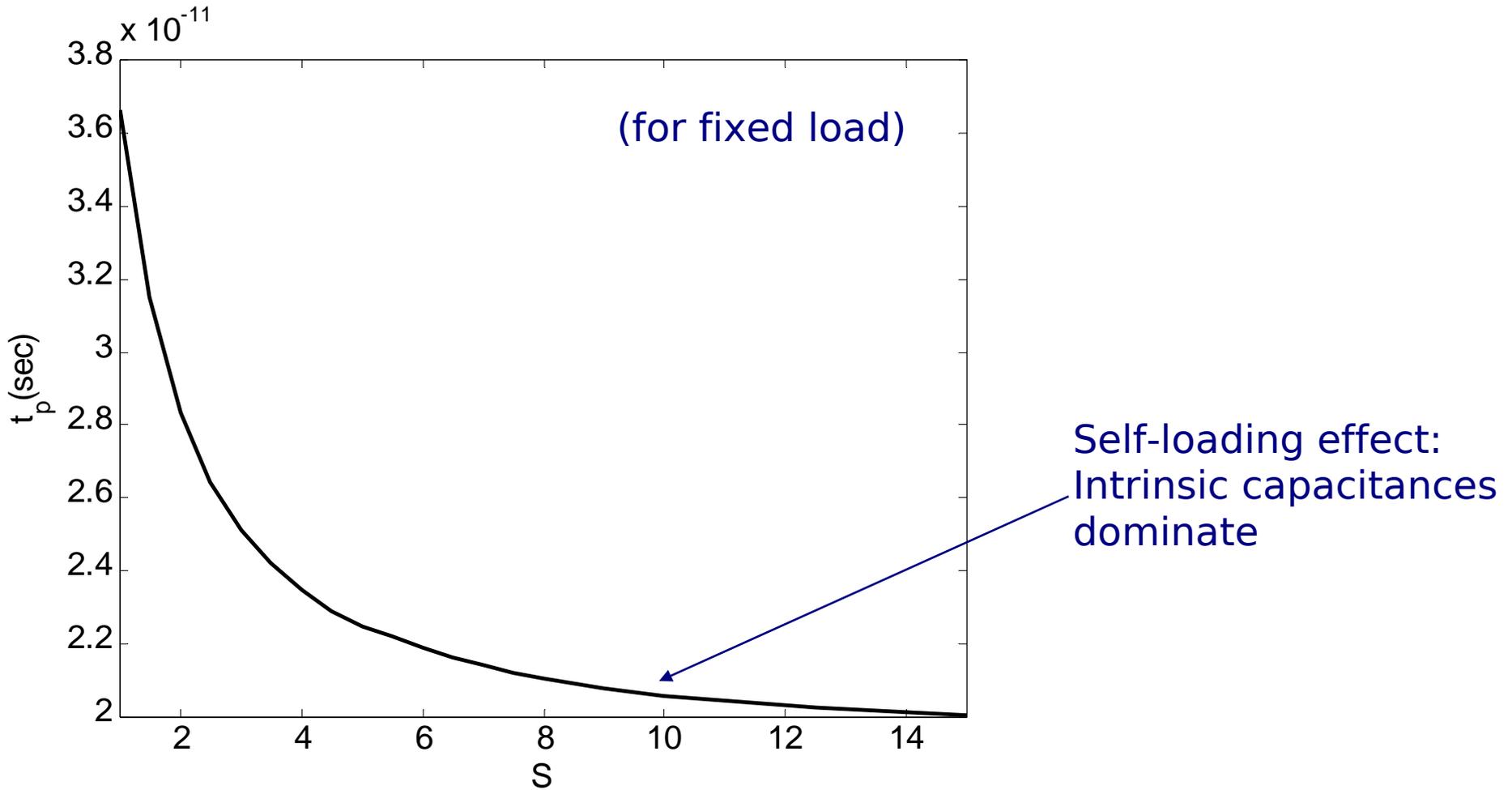
Diseño para mayor performance

- ❑ Mantener bajas las capacitancias.
- ❑ Aumentar los tamaños del transistor cuidando la capacidad de salida.
- ❑ Aumentar V_{DD} (????)

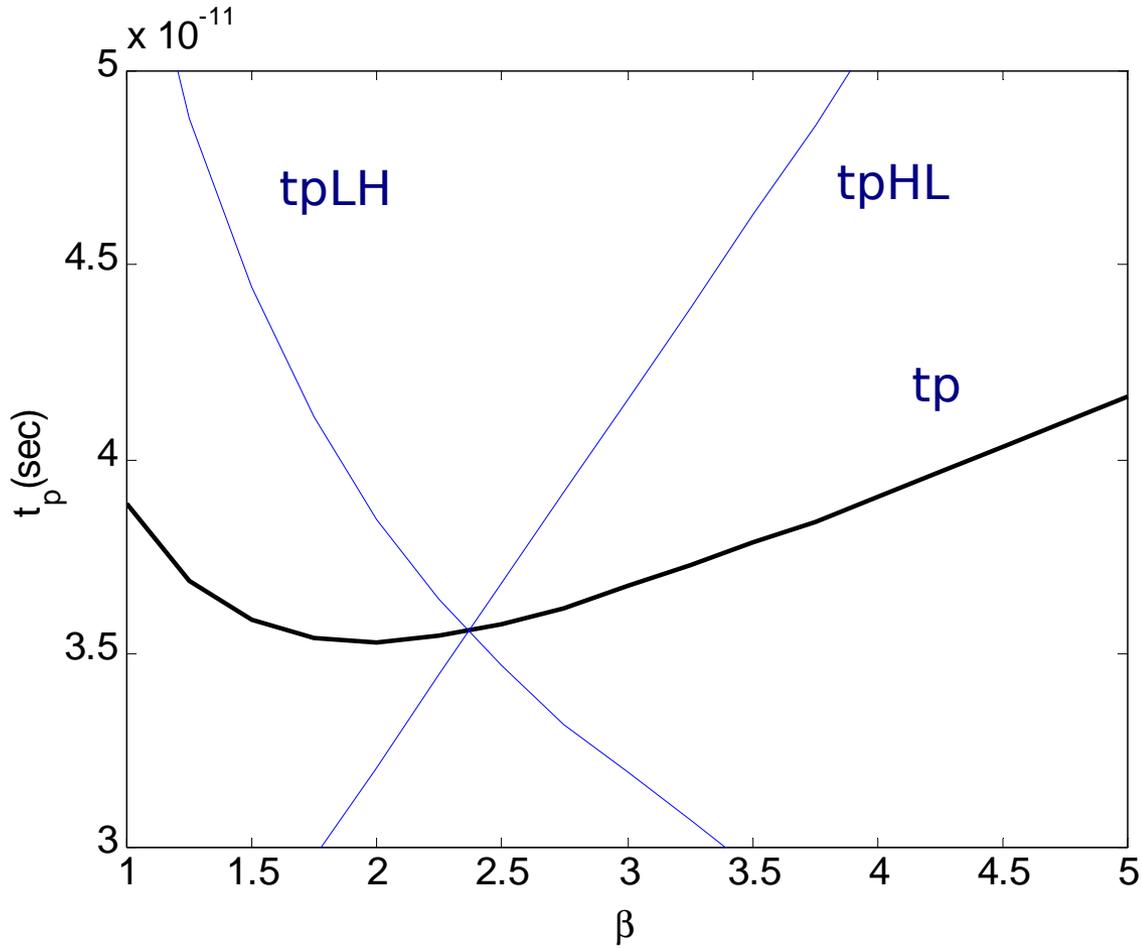
Delay as a function of V_{DD}



Device Sizing

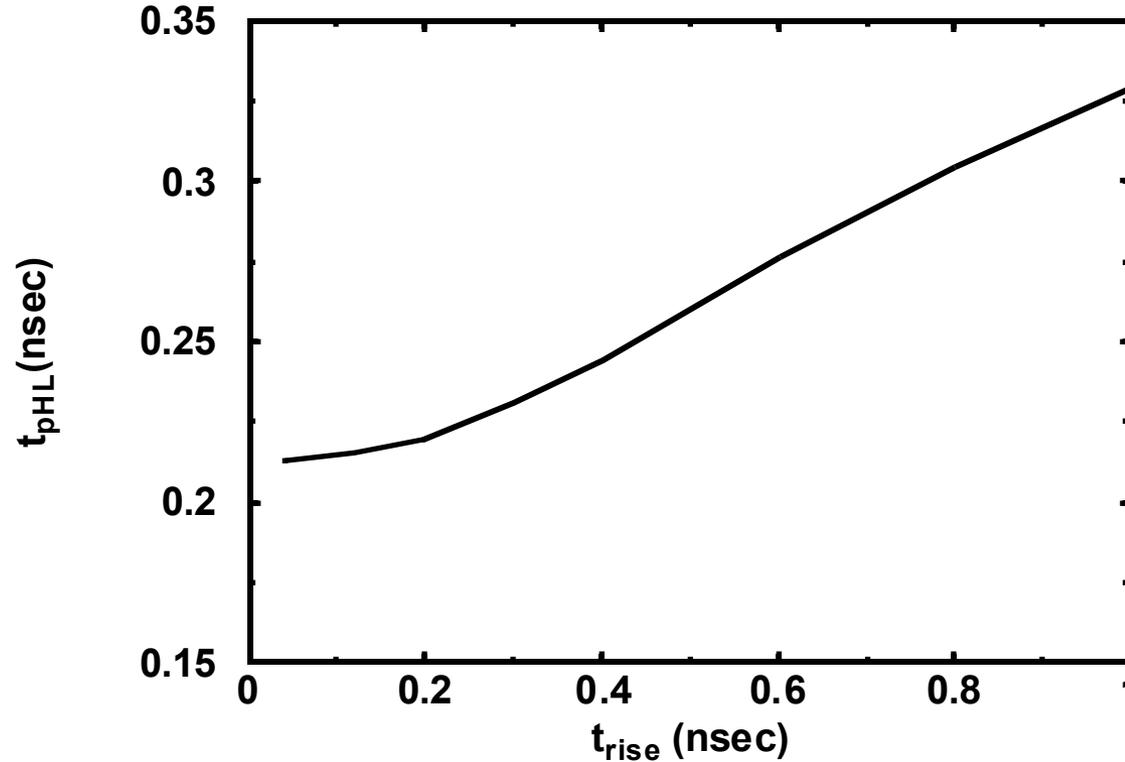


NMOS/PMOS ratio

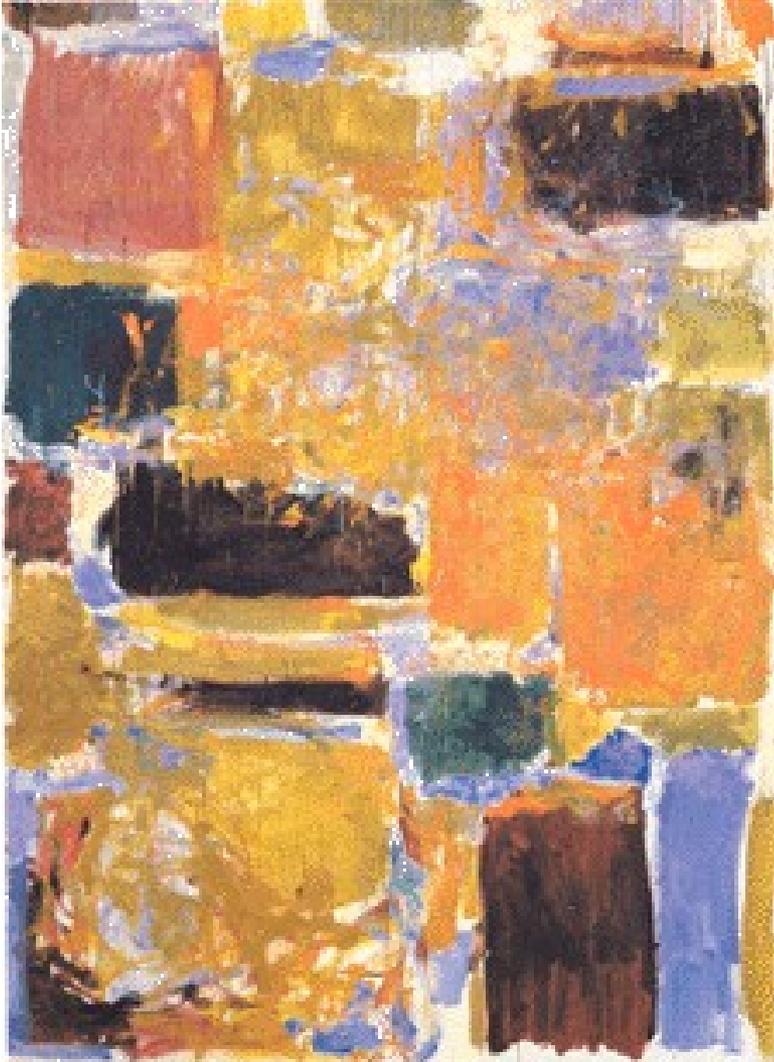


$$\beta = W_p/W_n$$

Impact of Rise Time on Delay

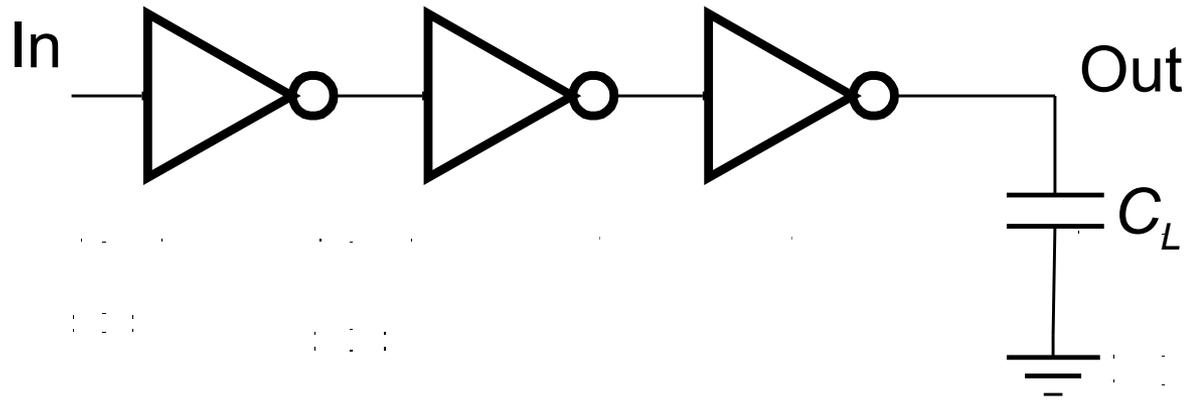


$$t_{pHL} = \sqrt{t_{pHL(step)}^2 + (t_r/2)^2}$$



Inverter Sizing

Inverter Chain



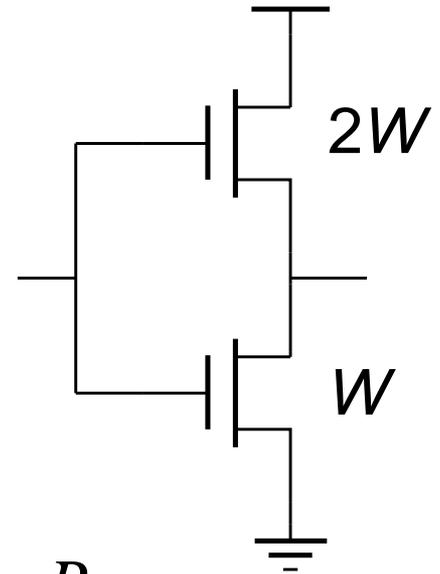
If C_L is given:

- How many stages are needed to minimize the delay?
- How to size the inverters?

May need some additional constraints.

Inverter Delay

- Minimum length devices
- Assume that for $W_P = 2W_N = 2W$
 - same pull-up and pull-down currents
 - approx. equal resistances $R_N = R_P$
 - approx. equal rise t_{pLH} and fall t_{pHL} delays
- Analyze as an RC network

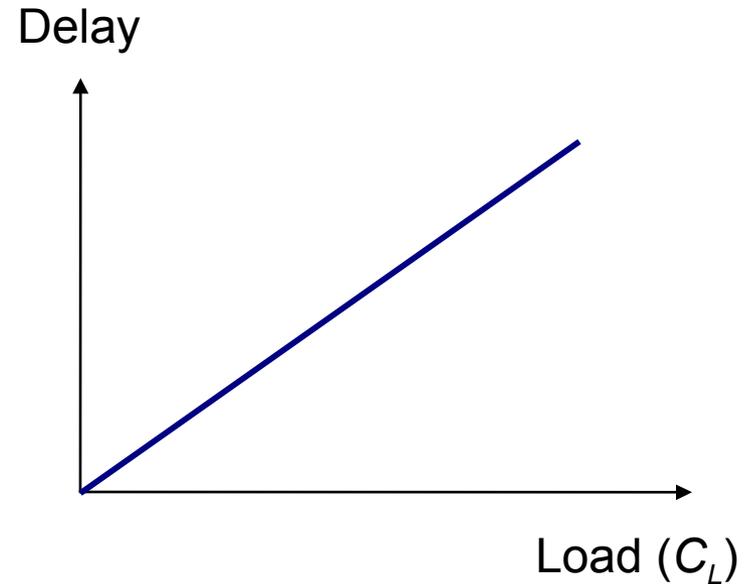
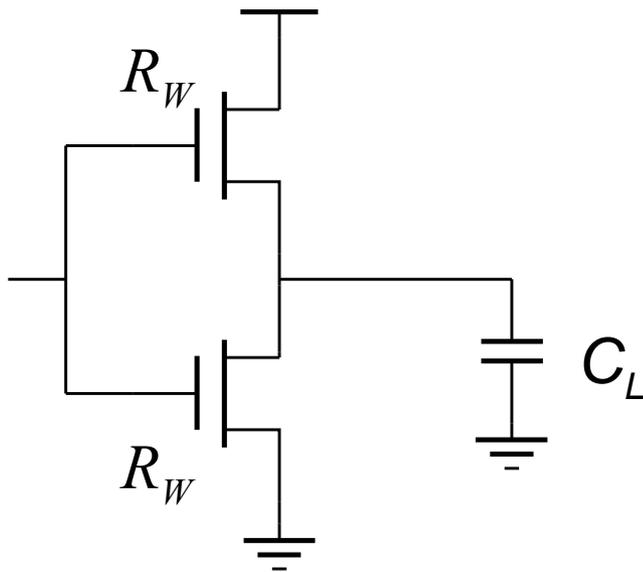


$$R_P = R_{unit} \left(\frac{W_P}{W_{unit}} \right)^{-1} \approx R_{unit} \left(\frac{W_N}{W_{unit}} \right)^{-1} = R_N = R_W$$

$$\text{Delay (D): } t_{pHL} = (\ln 2) R_N C_L \qquad t_{pLH} = (\ln 2) R_P C_L$$

$$\text{Load for the next stage: } C_{gin} = 3 \frac{W}{W_{unit}} C_{unit}$$

Inverter with Load

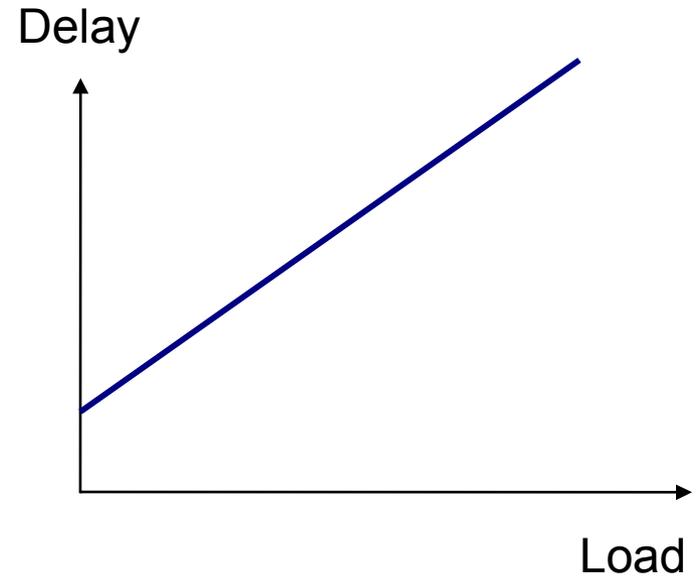
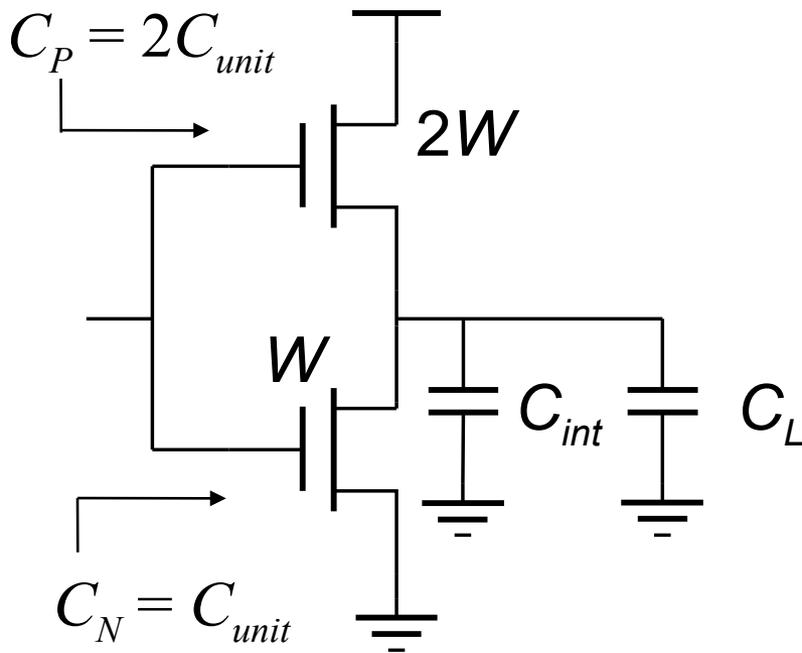


k is a constant, equal to 0.69

Assumptions: no load \rightarrow zero delay

$$W_{unit} = 1$$

Inverter with Load



$$\begin{aligned} \text{Delay} &= kR_W(C_{int} + C_L) = kR_W C_{int} + kR_W C_L = kR_W C_{int}(1 + C_L / C_{int}) \\ &= \text{Delay (Internal)} + \text{Delay (Load)} \end{aligned}$$

Delay Formula

$$\text{Delay} \sim R_W (C_{\text{int}} + C_L)$$

$$t_p = kR_W C_{\text{int}} \left(1 + C_L / C_{\text{int}}\right) = t_{p0} (1 + f / \gamma)$$

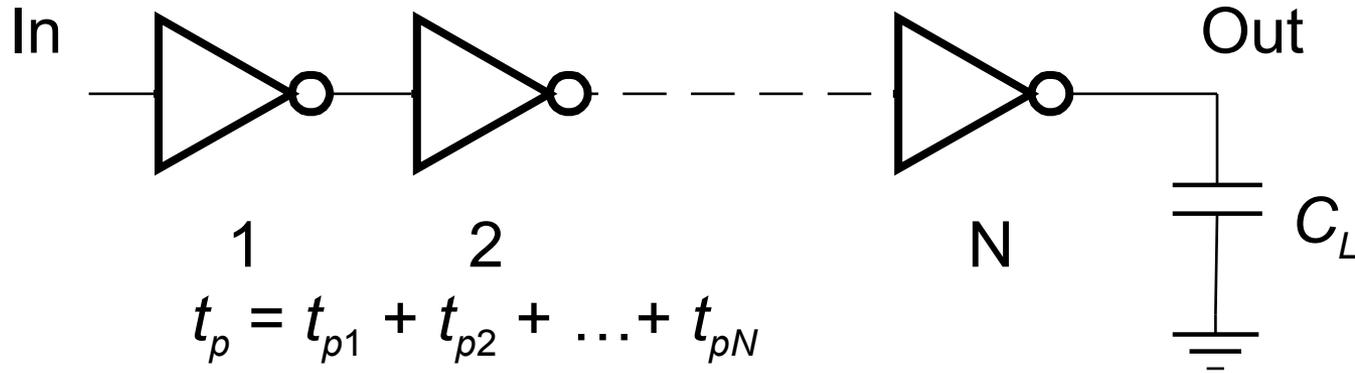
$$C_{\text{int}} = \gamma C_{\text{gin}} \text{ with } \gamma \approx 1$$

$$f = C_L / C_{\text{gin}} - \text{effective fanout}$$

$$R = R_{\text{unit}} / W ; C_{\text{int}} = WC_{\text{unit}}$$

$$t_{p0} = 0.69 R_{\text{unit}} C_{\text{unit}}$$

Apply to Inverter Chain



$$t_{pj} \sim R_{unit} C_{unit} \left(1 + \frac{C_{gin,j+1}}{\gamma C_{gin,j}} \right)$$

$$t_p = \sum_{j=1}^N t_{p,j} = t_{p0} \sum_{i=1}^N \left(1 + \frac{C_{gin,j+1}}{\gamma C_{gin,j}} \right), \quad C_{gin,N+1} = C_L$$

Optimal Tapering for Given N

Delay equation has $N - 1$ unknowns, $C_{gin,2} - C_{gin,N}$

Minimize the delay, find $N - 1$ partial derivatives

Result: $C_{gin,j+1}/C_{gin,j} = C_{gin,j}/C_{gin,j-1}$

Size of each stage is the geometric mean of two neighbors

$$C_{gin,j} = \sqrt{C_{gin,j-1} C_{gin,j+1}}$$

- each stage has the same effective fanout (C_{out}/C_{in})
- each stage has the same delay

Optimum Delay and Number of Stages

When each stage is sized by f and has same eff. fanout f :

$$f^N = F = C_L / C_{gin,1}$$

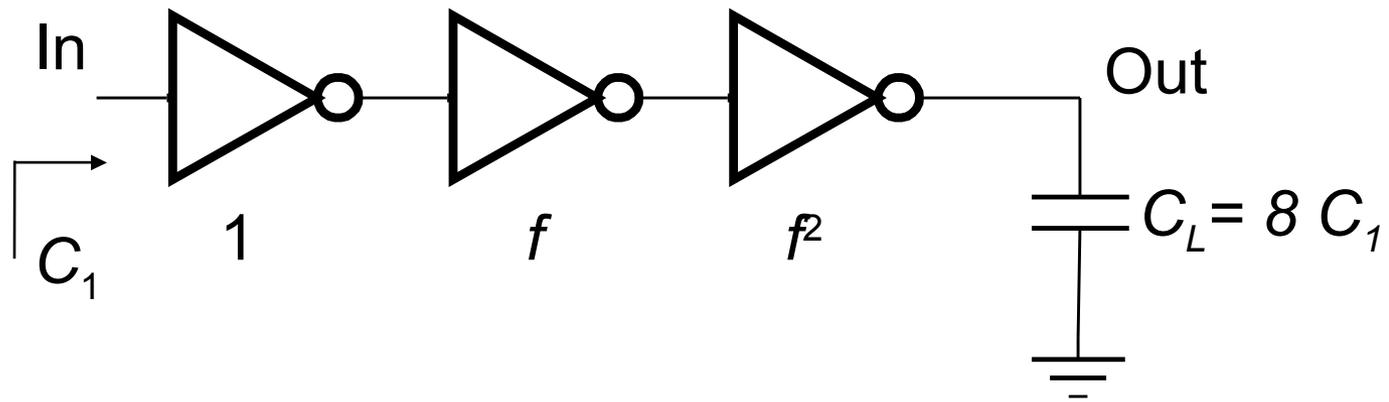
Effective fanout of each stage:

$$f = \sqrt[N]{F}$$

Minimum path delay

$$t_p = N t_{p0} \left(1 + \sqrt[N]{F} / \gamma \right)$$

Example



C_L/C_1 has to be evenly distributed across $N = 3$ stages:

$$f = \sqrt[3]{8} = 2$$

Optimum Number of Stages

For a given load, C_L and given input capacitance C_{in}
Find optimal sizing f

$$C_L = F \cdot C_{in} = f^N C_{in} \quad \text{with} \quad N = \frac{\ln F}{\ln f}$$

$$t_p = N t_{p0} \left(F^{1/N} / \gamma + 1 \right) = \frac{t_{p0} \ln F}{\gamma} \left(\frac{f}{\ln f} + \frac{\gamma}{\ln f} \right)$$

$$\frac{\partial t_p}{\partial f} = \frac{t_{p0} \ln F}{\gamma} \cdot \frac{\ln f - 1 - \gamma/f}{\ln^2 f} = 0$$

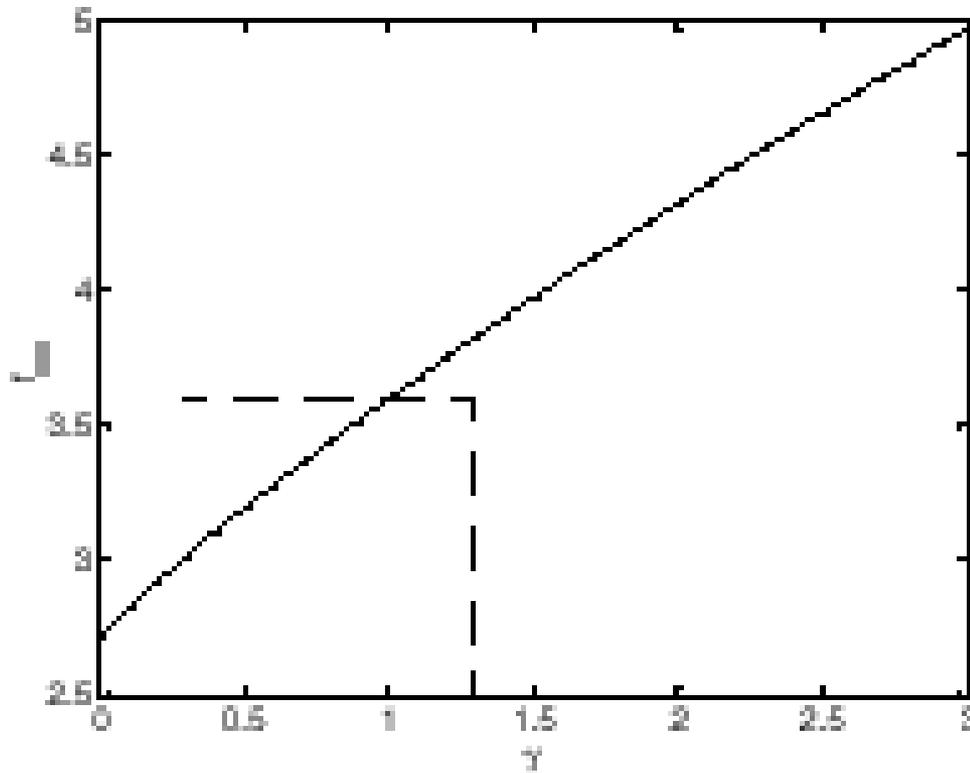
For $\gamma = 0$, $f = e$, $N = \ln F$

$$f = \exp(1 + \gamma/f)$$

Optimum Effective Fanout f

Optimum f for given process defined by γ

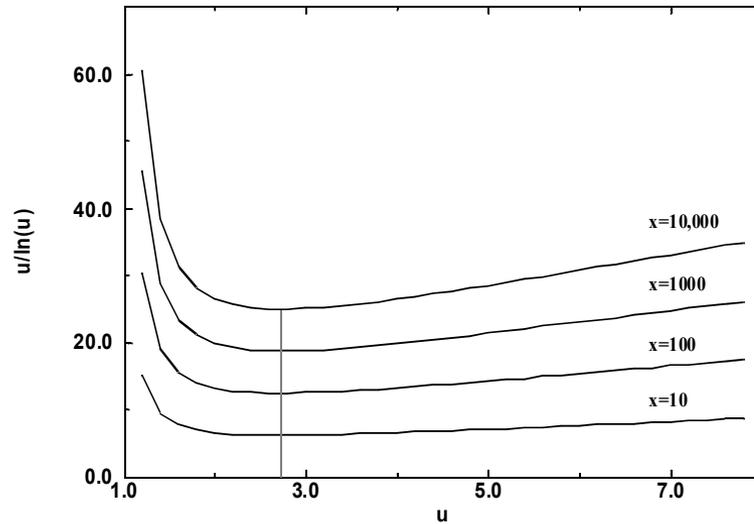
$$f = \exp(1 + \gamma / f)$$



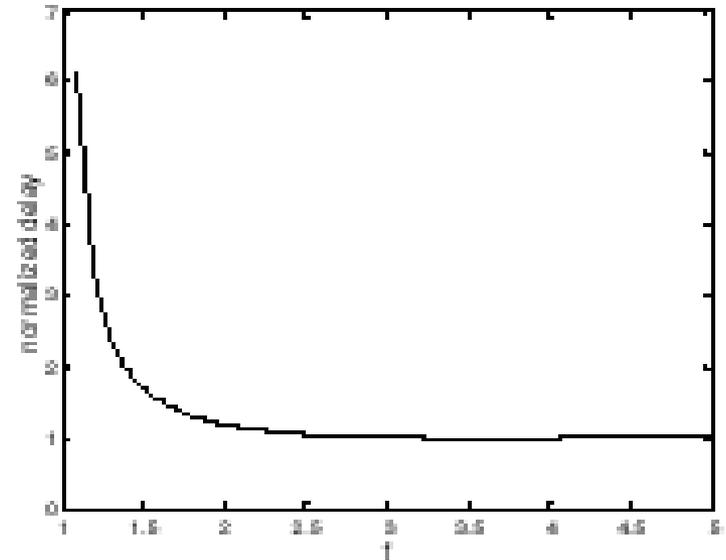
$f_{opt} = 3.6$
for $\gamma=1$

Impact of Self-Loading on t_p

No Self-Loading, $\gamma=0$



With Self-Loading $\gamma=1$

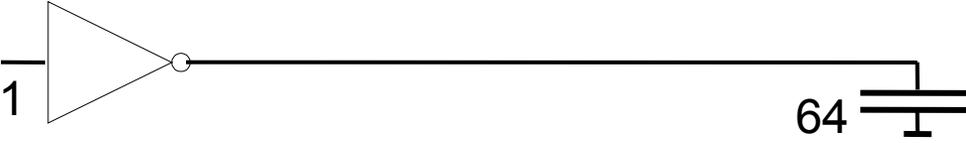
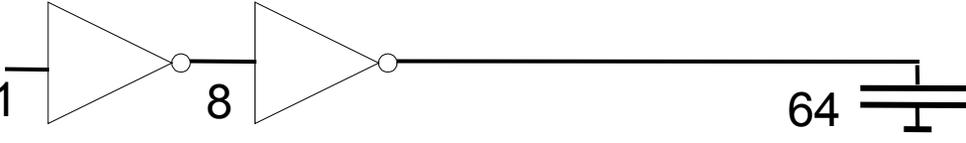
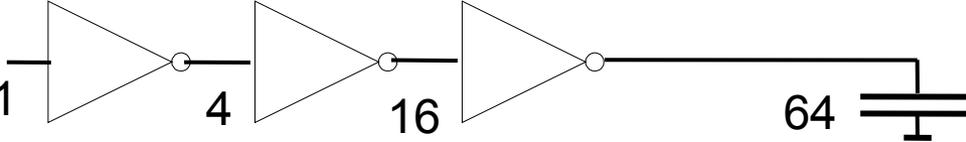
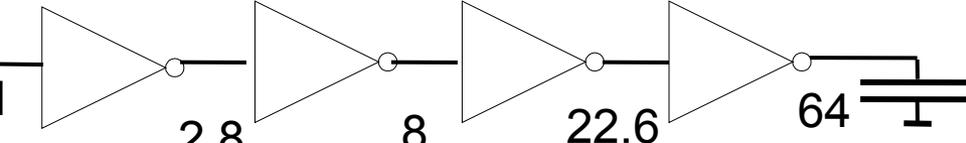


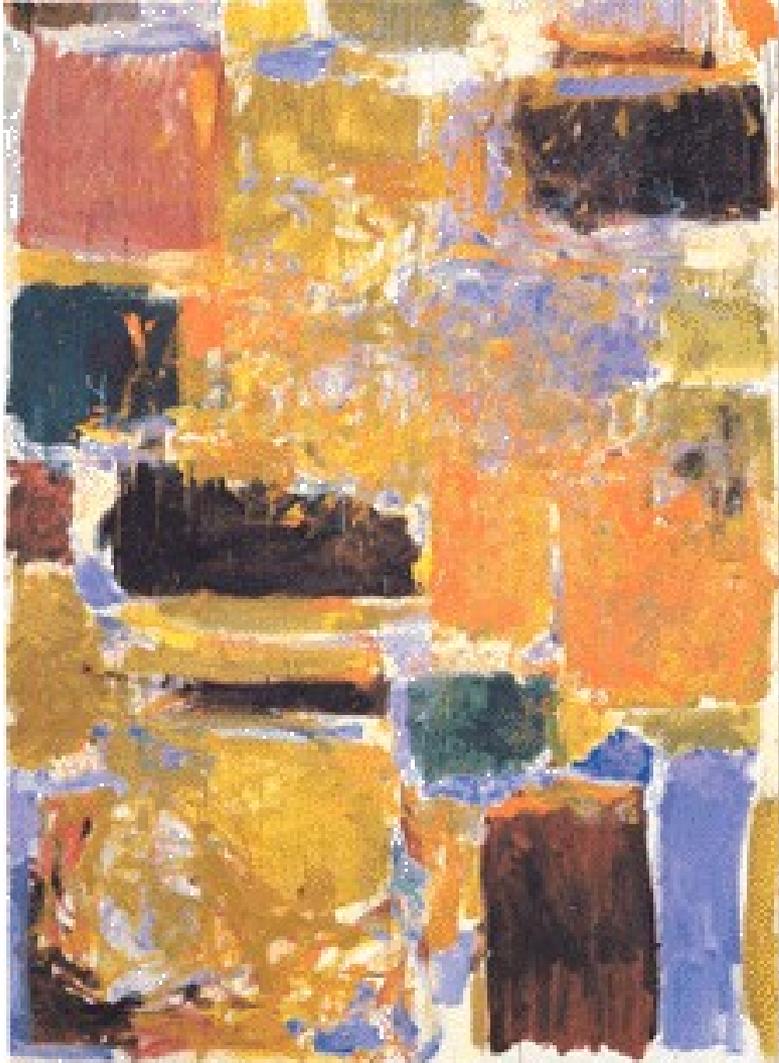
Normalized delay function of F

$$t_p = N t_{p0} \left(1 + \sqrt[N]{F / \gamma} \right)$$

<i>F</i>	Unbuffered	Two Stage	Inverter Chain
10	11	8.3	8.3
100	101	22	16.5
1000	1001	65	24.8
10,000	10,001	202	33.1

Buffer Design

	N	f	t_p
	1	64	65
	2	8	18
	3	4	15
	4	2.8	15.3



Power Dissipation

Where Does Power Go in CMOS?

- **Dynamic Power Consumption**

Charging and Discharging Capacitors

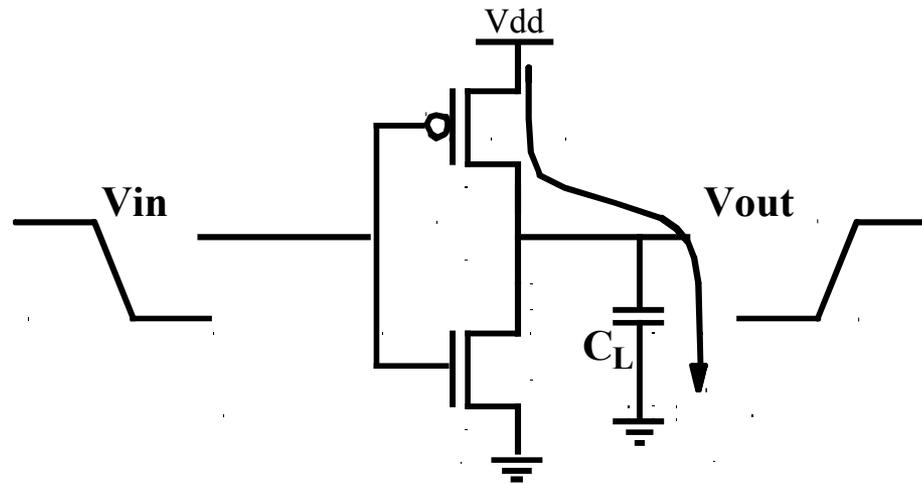
- **Short Circuit Currents**

Short Circuit Path between Supply Rails during Switching

- **Leakage**

Leaking diodes and transistors

Dynamic Power Dissipation

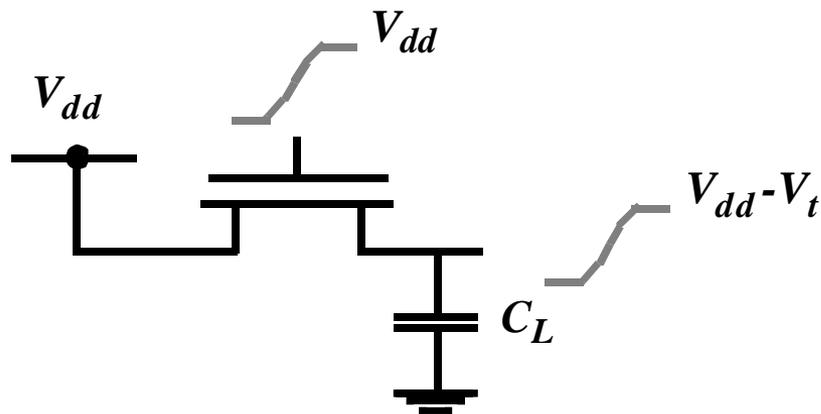


$$\text{Energy/transition} = C_L * V_{dd}^2$$

$$\text{Power} = \text{Energy/transition} * f = C_L * V_{dd}^2 * f$$

- Not a function of transistor sizes!
- Need to reduce C_L , V_{dd} , and f to reduce power.

Modification for Circuits with Reduced Swing

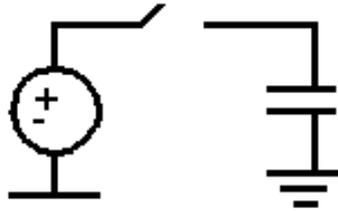


$$E_{0 \rightarrow 1} = C_L \cdot V_{dd} \cdot (V_{dd} - V_t)$$

- Can exploit reduced swing to lower power (e.g., reduced bit-line swing in memory)

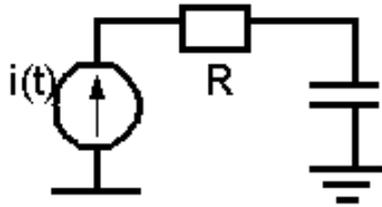
Adiabatic Charging

Charging a capacitor



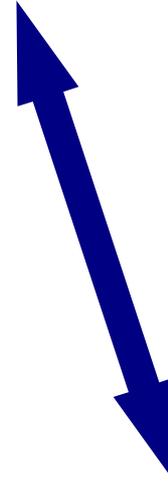
$$CV_{dd}^2/2$$

Consider



$$v_c = \frac{1}{C} \cdot \int_0^T i dt = \frac{1}{C} \cdot I_{av} \cdot T \quad I_{av} = \frac{C \cdot v_c}{T}$$

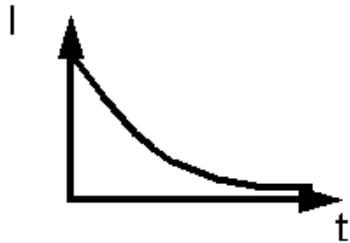
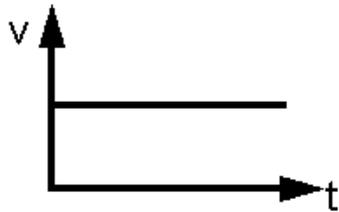
$$E_{dis} = R \cdot \int_0^T i^2(t) dt \geq R \cdot \int_0^T I_{av}^2 dt = R \cdot I_{av}^2 \cdot T = \frac{RC}{T} \cdot C \cdot V_c^2$$



Adiabatic Charging

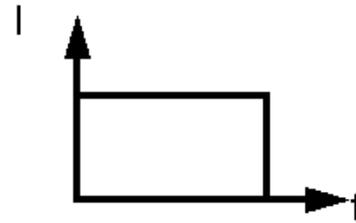
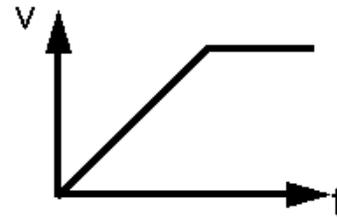
$$V_I = RI + V_c = RC \frac{dv_c}{dt} + V_c$$

$V_I = \text{cst} \rightarrow$ Exponential current



$$E_R = CV_c^2 / 2$$

$I = I_{av} \rightarrow$ Linear ramp on V_I



wins if $T > 2RC$

mimimal energy

$$E_R = RC/T CV_c^2$$

Node Transition Activity and Power

- Consider switching a CMOS gate for N clock cycles

$$E_N = C_L \cdot V_{dd}^2 \cdot n(N)$$

E_N : the energy consumed for N clock cycles

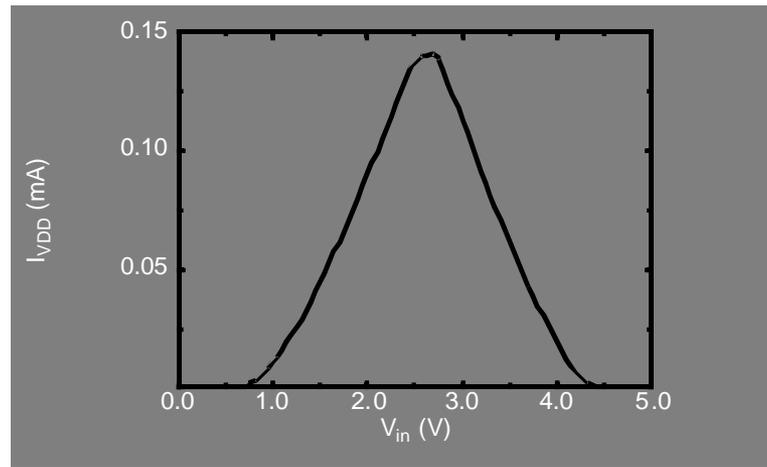
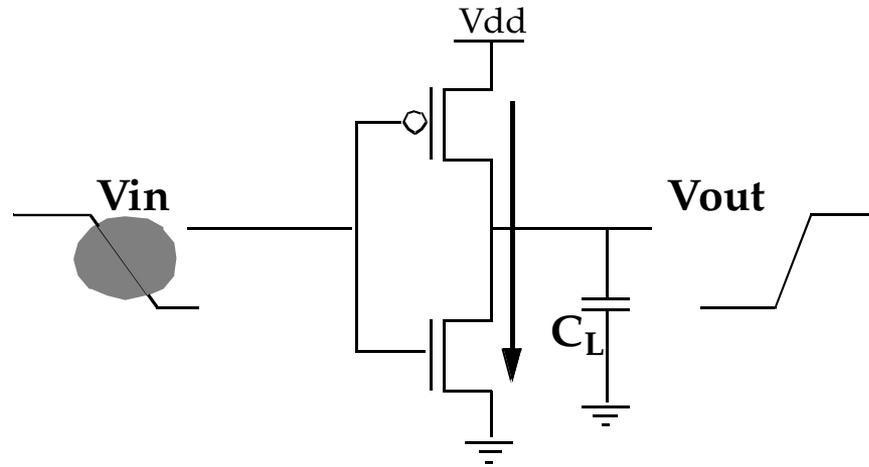
$n(N)$: the number of 0->1 transition in N clock cycles

$$P_{avg} = \lim_{N \rightarrow \infty} \frac{E_N}{N} \cdot f_{clk} = \left(\lim_{N \rightarrow \infty} \frac{n(N)}{N} \right) \cdot C_L \cdot V_{dd}^2 \cdot f_{clk}$$

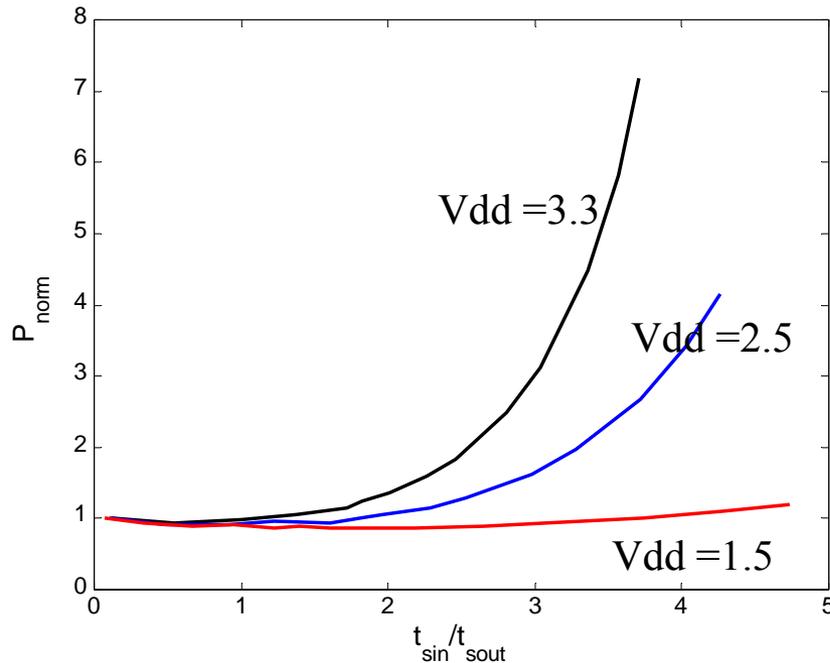
$$\alpha_{0 \rightarrow 1} = \lim_{N \rightarrow \infty} \frac{n(N)}{N}$$

$$P_{avg} = \alpha_{0 \rightarrow 1} \cdot C_L \cdot V_{dd}^2 \cdot f_{clk}$$

Short Circuit Currents



Minimizing Short-Circuit Power



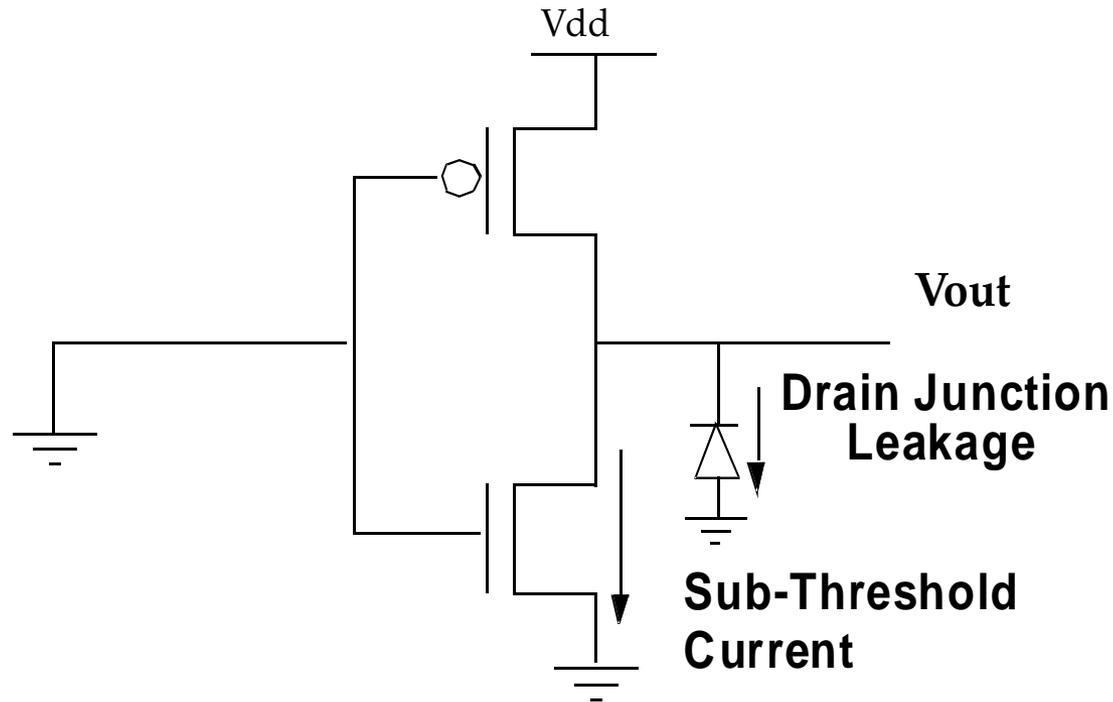
- Keep the input and output rise/fall times the same (< 10% of Total Consumption)

from [Veendrick84]

(*IEEE Journal of Solid-State Circuits*, August 1984)

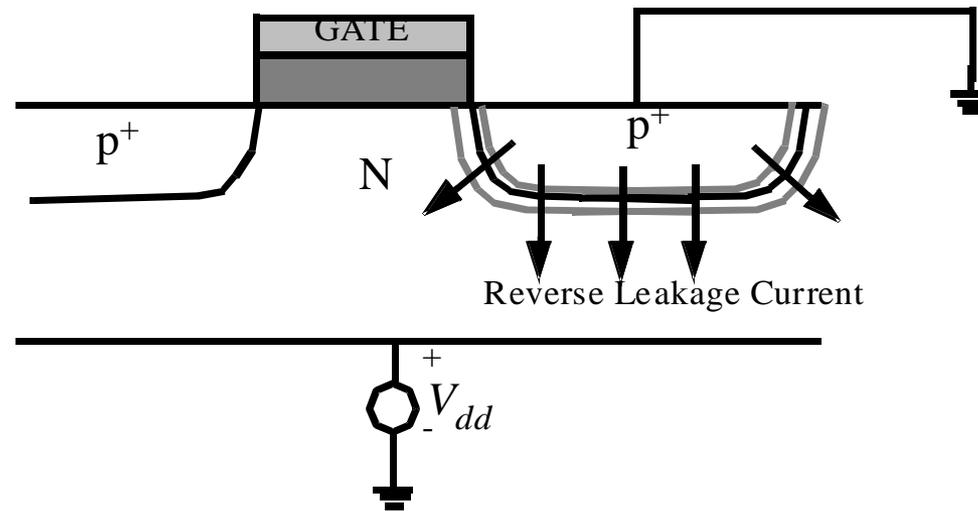
- If $V_{\text{dd}} < V_{\text{tn}} + |V_{\text{tp}}|$ then short-circuit power can be *eliminated!*

Leakage



Sub-threshold current one of most compelling issues in low-energy circuit design!

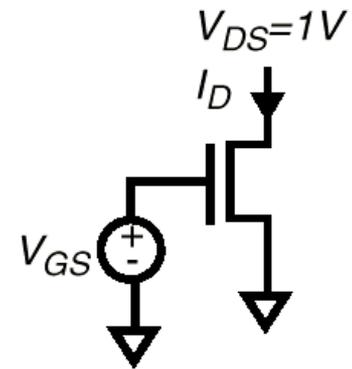
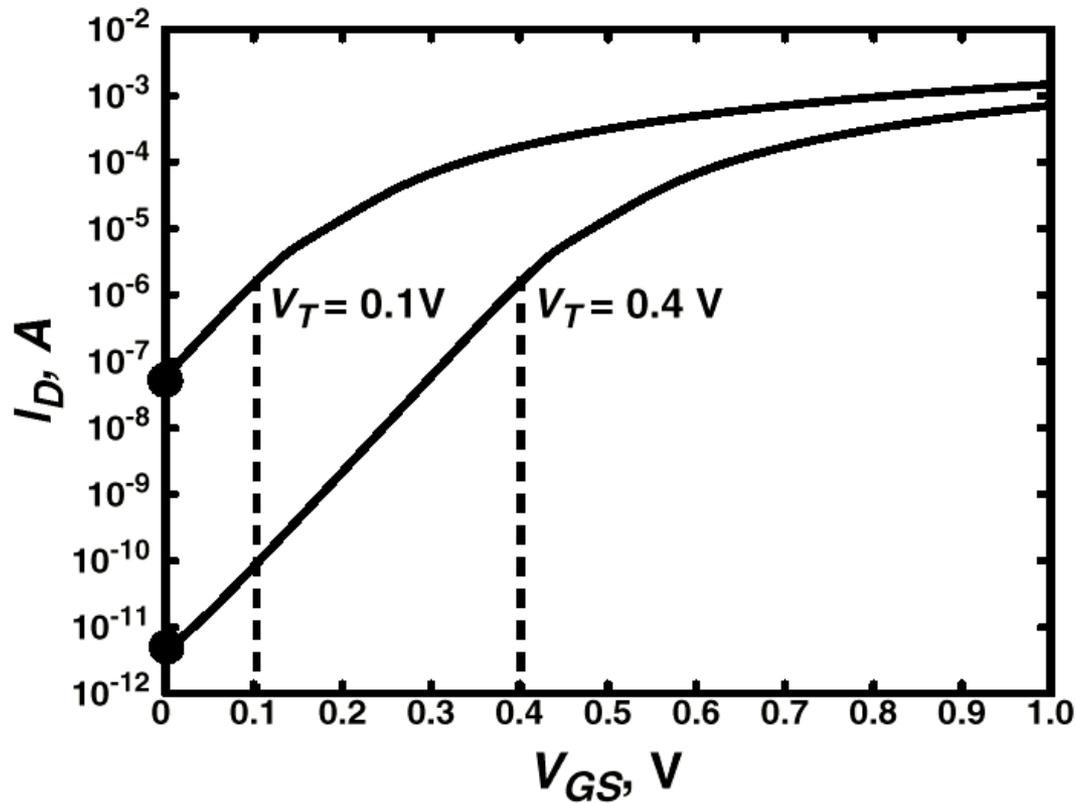
Reverse-Biased Diode Leakage



$$I_{DL} = J_S \times A$$

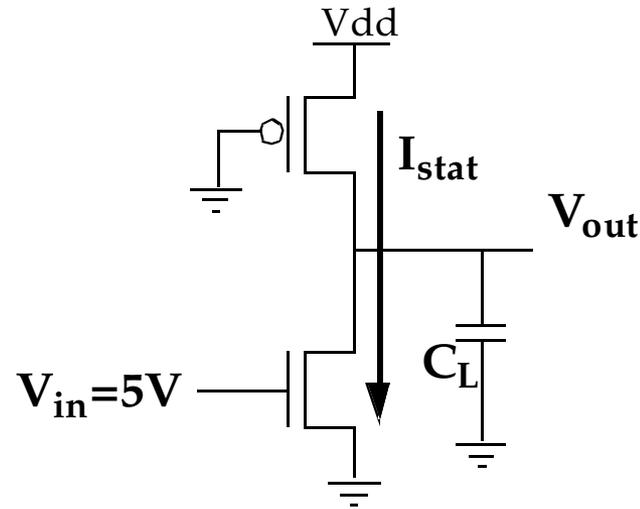
J_S = 10-100 pA/μm² at 25 deg C for 0.25μm CMOS
J_S doubles for every 9 deg C!

Subthreshold Leakage Component



- Leakage control is critical for low-voltage operation

Static Power Consumption



$$P_{stat} = P_{(I_n=1)} \cdot V_{dd} \cdot I_{stat}$$

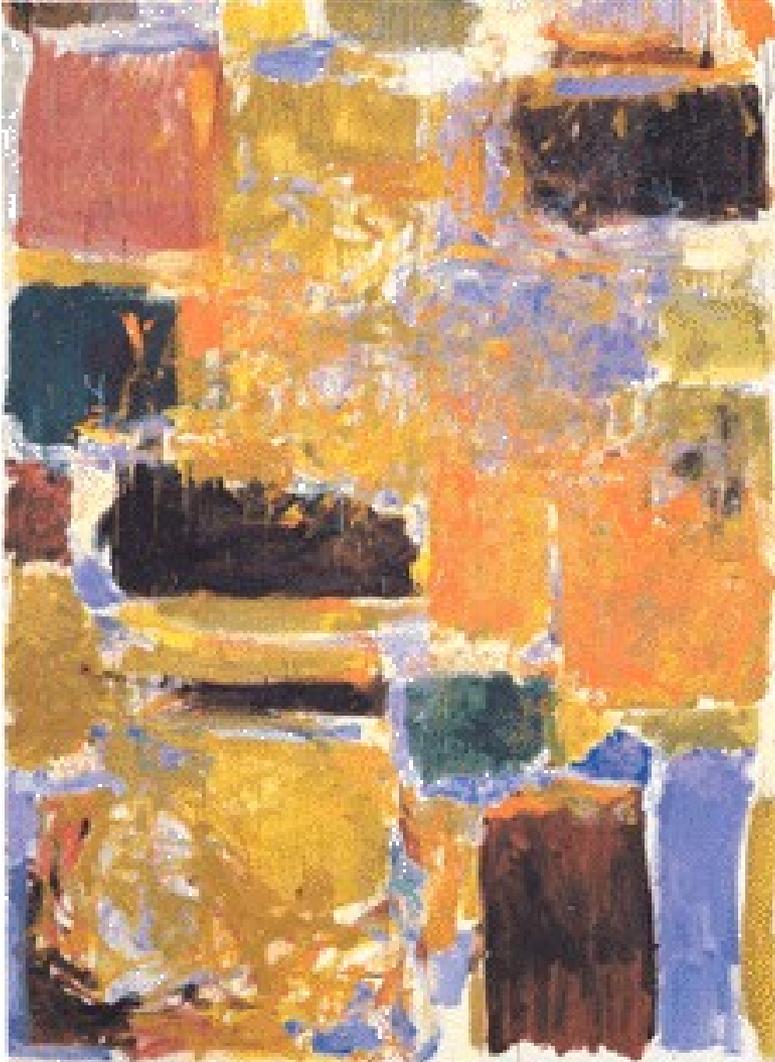
Wasted energy ...

Should be avoided in almost all cases,

but could help reducing energy in others (e.g. sense amps)

Principles for Power Reduction

- Prime choice: Reduce voltage!
 - Recent years have seen an acceleration in supply voltage reduction
 - Design at very low voltages still open question
- Reduce switching activity
- Reduce physical capacitance
 - Device Sizing: for $F=20$
 - $f_{opt}(\text{energy})=3.53$, $f_{opt}(\text{performance})=4.47$



Impact of Technology Scaling

Goals of Technology Scaling

- Make things cheaper:
 - Want to sell more functions (transistors) per chip for the same money
 - Build same products cheaper, sell the same part for less money
 - Price of a transistor has to be reduced
- But also want to be faster, smaller, lower power

Technology Scaling

- Goals of scaling the dimensions by 30%:
 - Reduce gate delay by 30% (increase operating frequency by 43%)
 - Double transistor density
 - Reduce energy per transition by 65% (50% power savings @ 43% increase in frequency)
- Die size used to increase by 14% per generation
- Technology generation spans 2-3 years

Technology Generations

Table 2. Time overlap of semiconductor technology generations.

	95	96	97	98	99	00	01	02	03	04	05	06	07	08	09	10	11	12
350 nm		1	2	3	4	5												
250 nm	-2	-1	1	2	3	4	5											
180 nm	-4	-3	-2	-1	1	2	3	4	5									
150 nm	-6	-5	-4	-3	-2	-1	1	2	3	4	5							
130 nm	-8	-7	-6	-5	-4	-3	-2	-1	1	2	3	4	5					
100 nm	-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1	1	2	3	4	5		
70 nm				-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1	1	2	3	
50 nm							-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1	1

Technology Evolution (2000 data)

International Technology Roadmap for Semiconductors

Year of Introduction	1999	2000	2001	2004	2008	2011	2014
Technology node [nm]	180		130	90	60	40	30
Supply [V]	1.5-1.8	1.5-1.8	1.2-1.5	0.9-1.2	0.6-0.9	0.5-0.6	0.3-0.6
Wiring levels	6-7	6-7	7	8	9	9-10	10
Max frequency [GHz], Local-Global	1.2	1.6-1.4	2.1-1.6	3.5-2	7.1-2.5	11-3	14.9-3.6
Max μP power [W]	90	106	130	160	171	177	186
Bat. power [W]	1.4	1.7	2.0	2.4	2.1	2.3	2.5

Node years: 2007/65nm, 2010/45nm, 2013/33nm, 2016/23nm

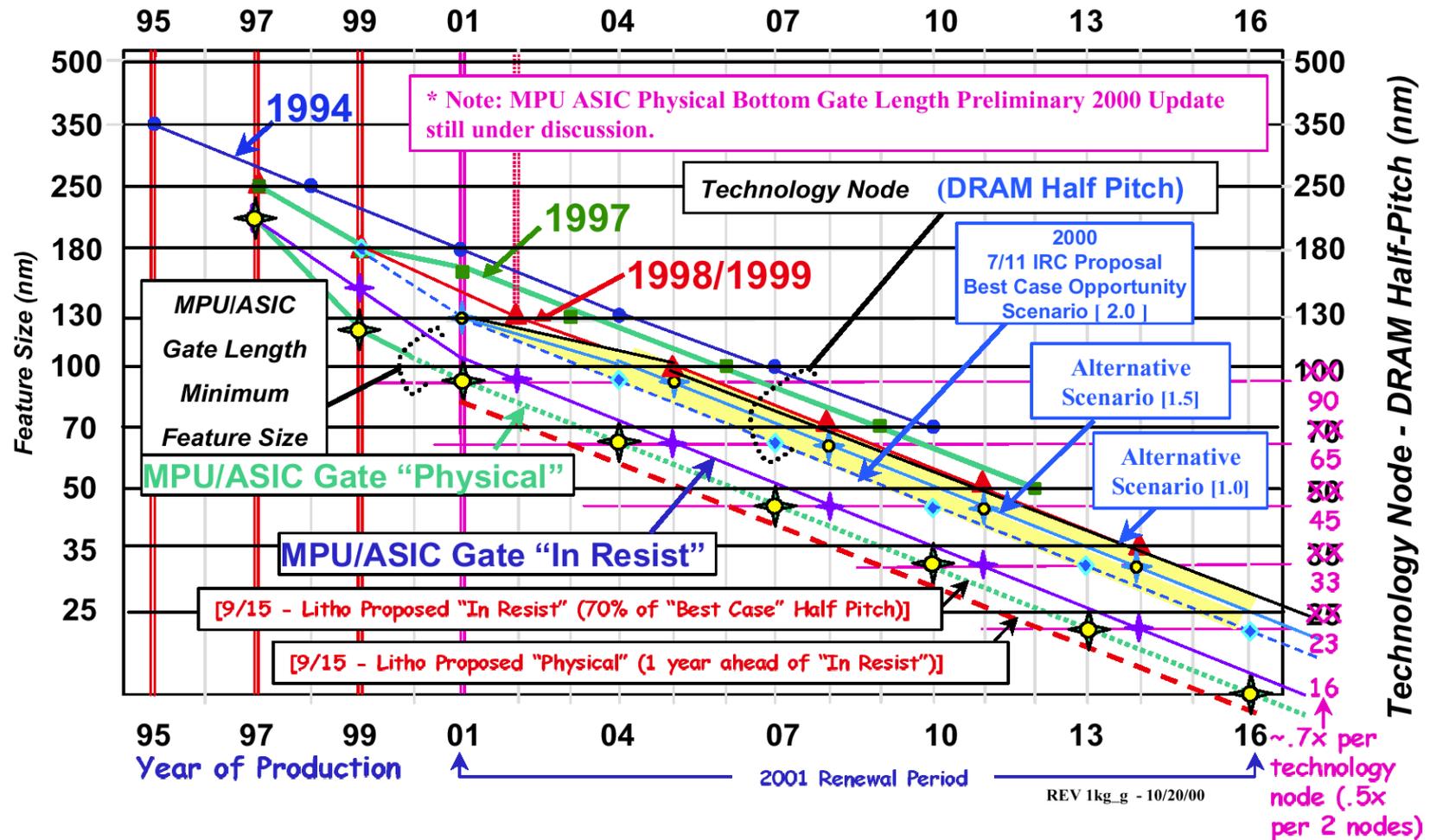
Technology Evolution (1999)

Year of Introduction	1994	1997	2000	2003	2006	2009
Channel length (μm)	0.4	0.3	0.25	0.18	0.13	0.1
Gate oxide (nm)	12	7	6	4.5	4	4
V_{DD} (V)	3.3	2.2	2.2	1.5	1.5	1.5
V_T (V)	0.7	0.7	0.7	0.6	0.6	0.6
NMOS I_{Dsat} (mA/ μm) (@ $V_{GS} = V_{DD}$)	0.35	0.27	0.31	0.21	0.29	0.33
PMOS I_{Dsat} (mA/ μm) (@ $V_{GS} = V_{DD}$)	0.16	0.11	0.14	0.09	0.13	0.16

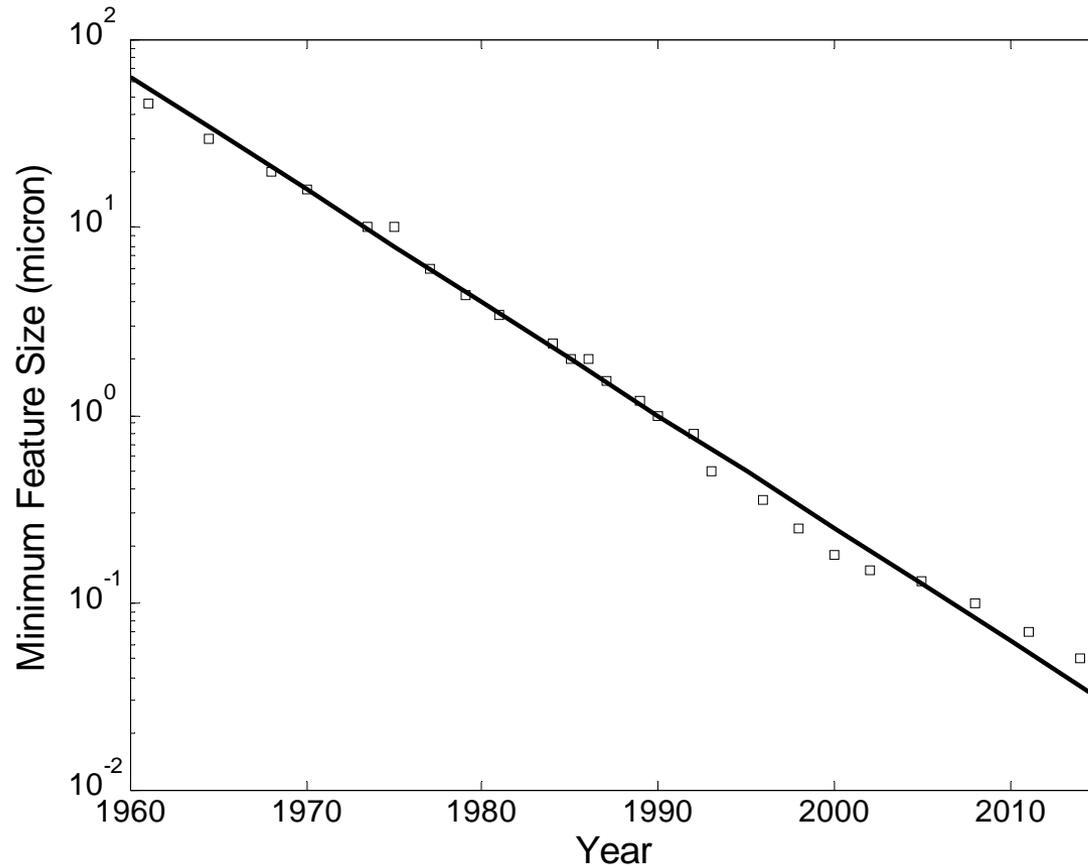
ITRS Technology Roadmap

Acceleration Continues

(Including MPU/ASIC "Physical Gate Length" Proposal)

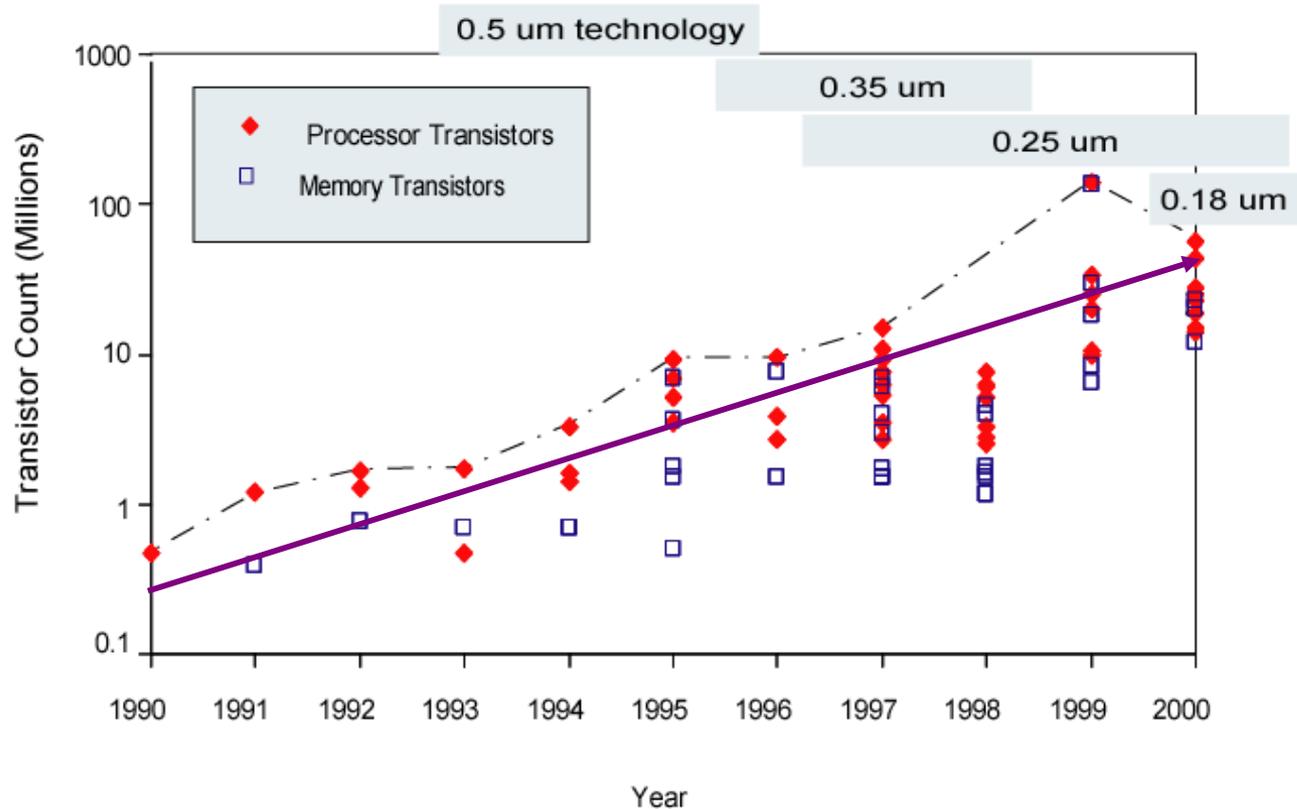


Technology Scaling (1)



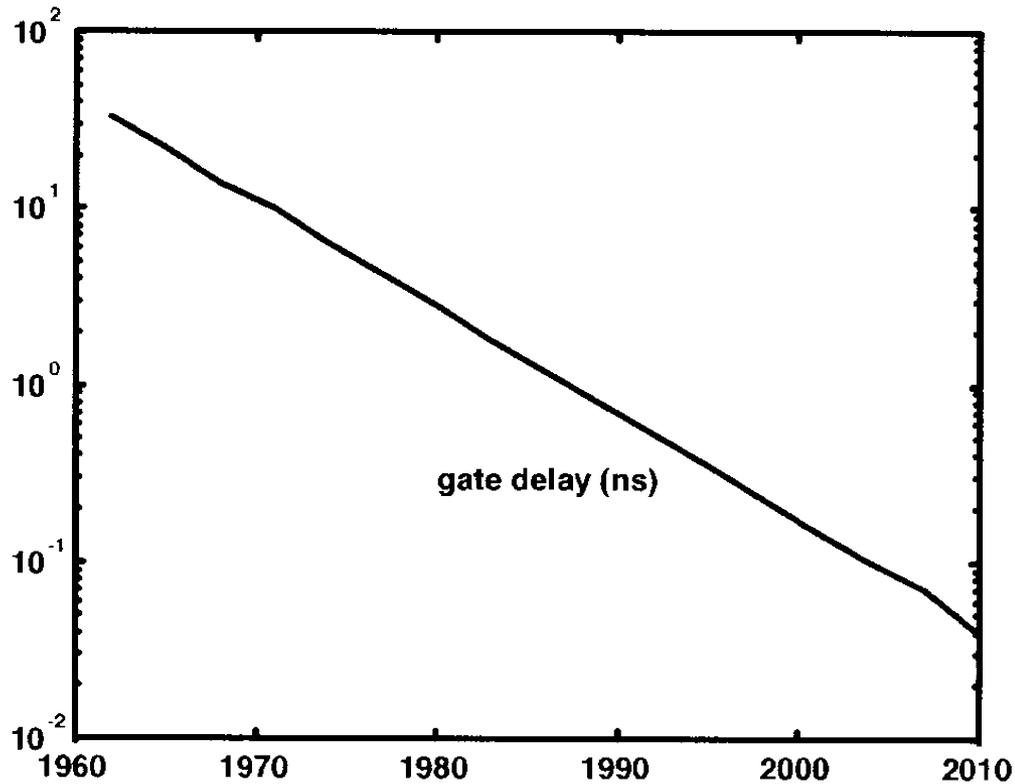
Minimum Feature Size

Technology Scaling (2)



Number of components per chip

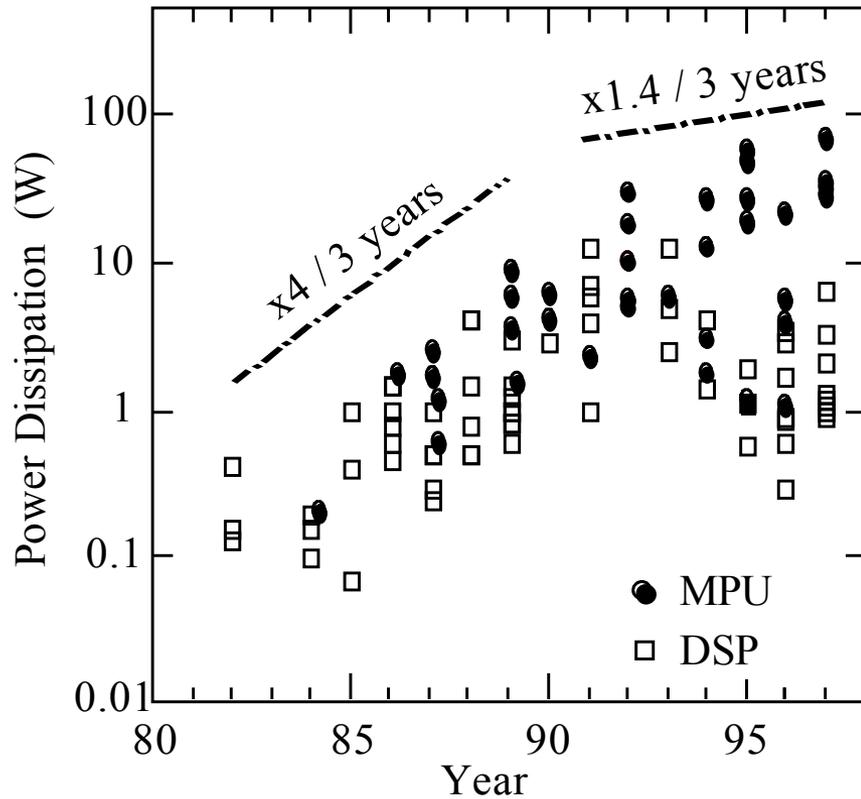
Technology Scaling (3)



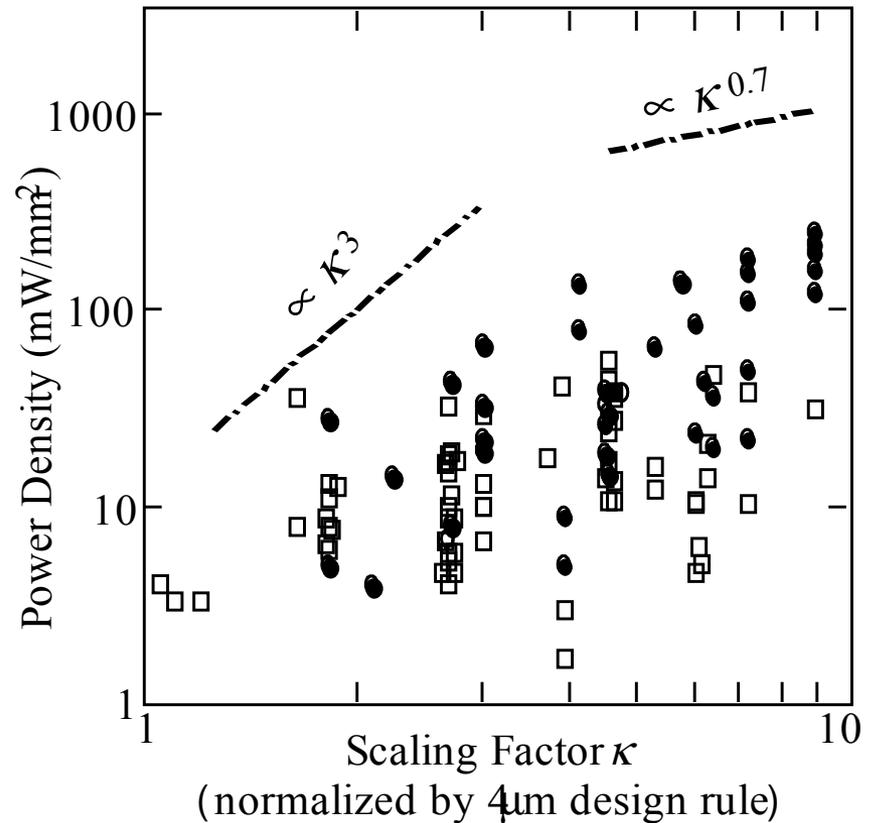
t_p decreases by 13%/year
50% every 5 years!

Propagation Delay

Technology Scaling (4)



(a) Power dissipation vs. year.



(b) Power density vs. scaling factor.

From Kuroda

Technology Scaling Models

- **Full Scaling (Constant Electrical Field)**

ideal model — dimensions and voltage scale together by the same factor S

- **Fixed Voltage Scaling**

most common model until recently —
only dimensions scale, voltages remain constant

- **General Scaling**

most realistic for today's situation —
voltages and dimensions scale with different factors

Scaling Relationships for Long Channel Devices

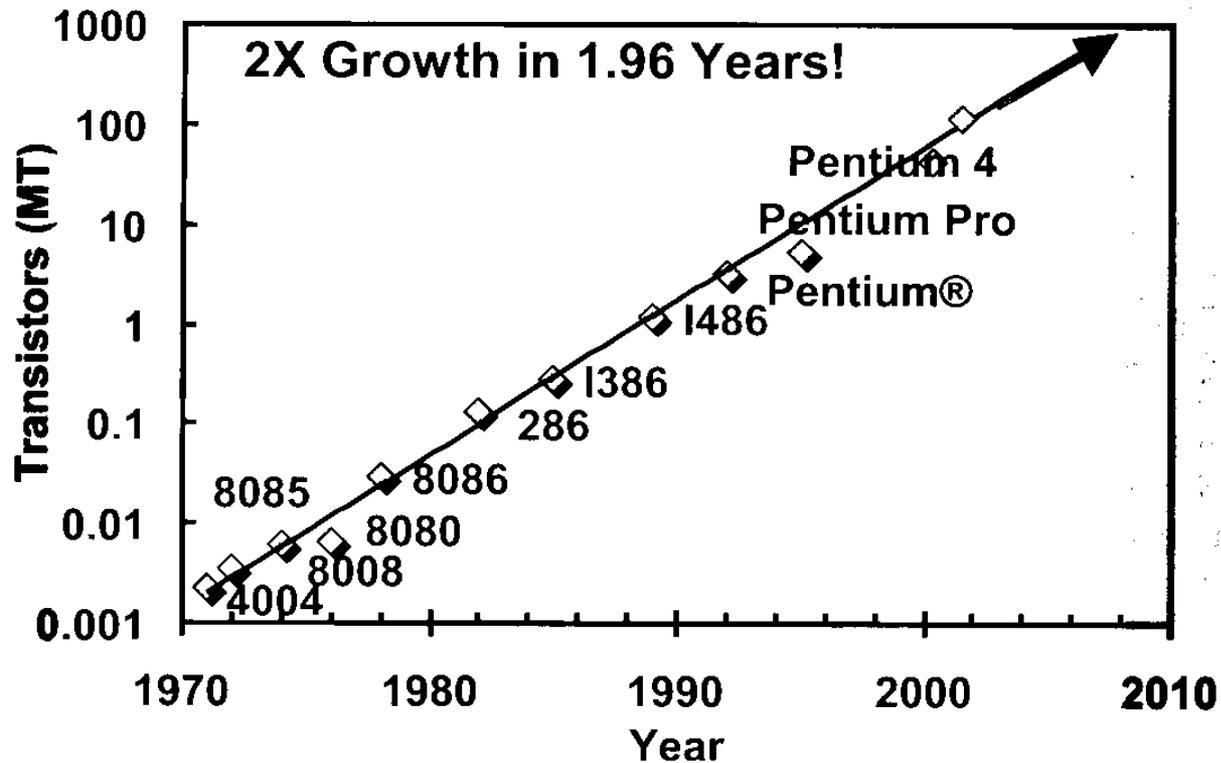
Parameter	Relation	Full Scaling	General Scaling	Fixed Voltage Scaling
W, L, t_{ox}		$1/S$	$1/S$	$1/S$
V_{DD}, V_T		$1/S$	$1/U$	1
N_{SUB}	V/W_{depl}^2	S	S^2/U	S^2
Area/Device	WL	$1/S^2$	$1/S^2$	$1/S^2$
C_{ox}	$1/t_{ox}$	S	S	S
C_L	$C_{ox}WL$	$1/S$	$1/S$	$1/S$
k_n, k_p	$C_{ox}W/L$	S	S	S
I_{av}	$k_{n,p} V^2$	$1/S$	S/U^2	S
t_p (intrinsic)	$C_L V / I_{av}$	$1/S$	U/S^2	$1/S^2$
P_{av}	$C_L V^2 / t_p$	$1/S^2$	S/U^3	S
PDP	$C_L V^2$	$1/S^3$	$1/SU^2$	$1/S$

Transistor Scaling

(velocity-saturated devices)

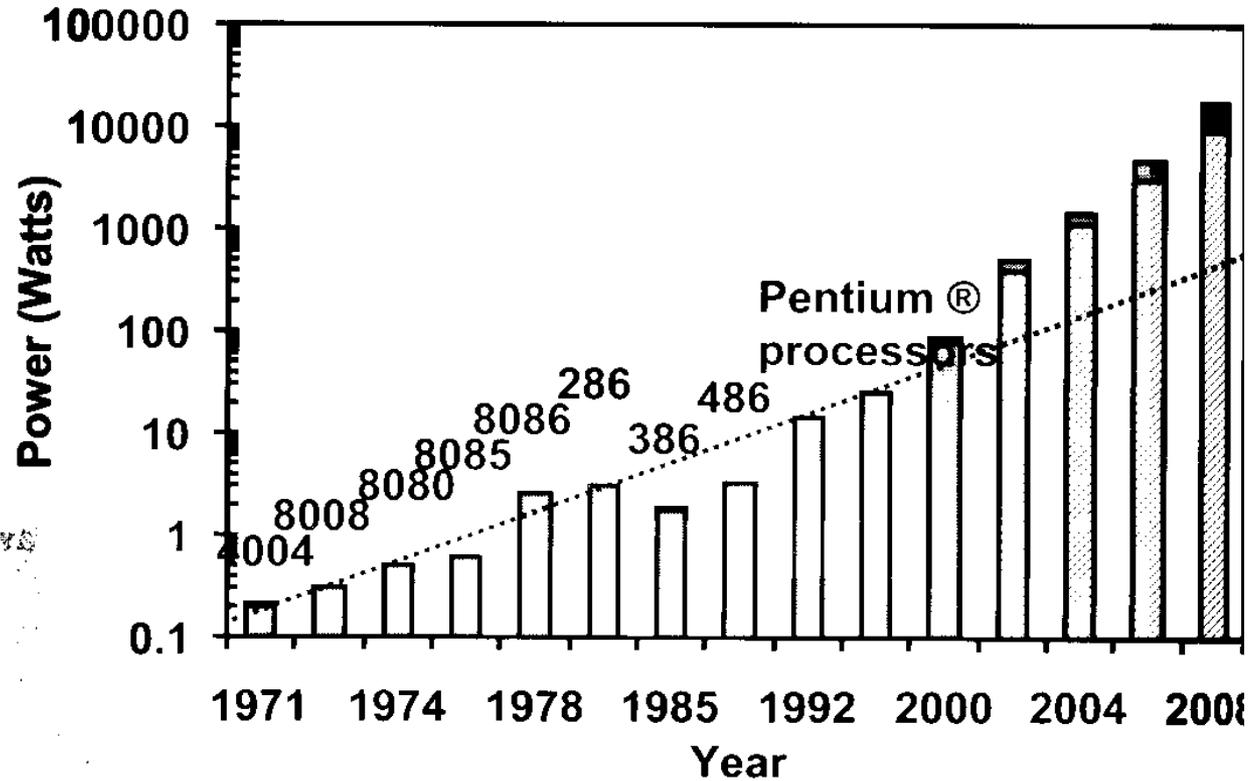
Parameter	Relation	Full Scaling	General Scaling	Fixed-Voltage Scaling
W, L, t_{ox}		$1/S$	$1/S$	$1/S$
V_{DD}, V_T		$1/S$	$1/U$	1
N_{SUB}	V/W_{depl}^2	S	S^2/U	S^2
Area/Device	WL	$1/S^2$	$1/S^2$	$1/S^2$
C_{ox}	$1/t_{ox}$	S	S	S
C_{gate}	$C_{ox}WL$	$1/S$	$1/S$	$1/S$
k_n, k_p	$C_{ox}W/L$	S	S	S
I_{sat}	$C_{ox}WV$	$1/S$	$1/U$	1
Current Density	$I_{sat}/Area$	S	S^2/U	S^2
R_{on}	V/I_{sat}	1	1	1
Intrinsic Delay	$R_{on}C_{gate}$	$1/S$	$1/S$	$1/S$
P	$I_{sat}V$	$1/S^2$	$1/U^2$	1
Power Density	$P/Area$	1	S^2/U^2	S^2

μ Processor Scaling



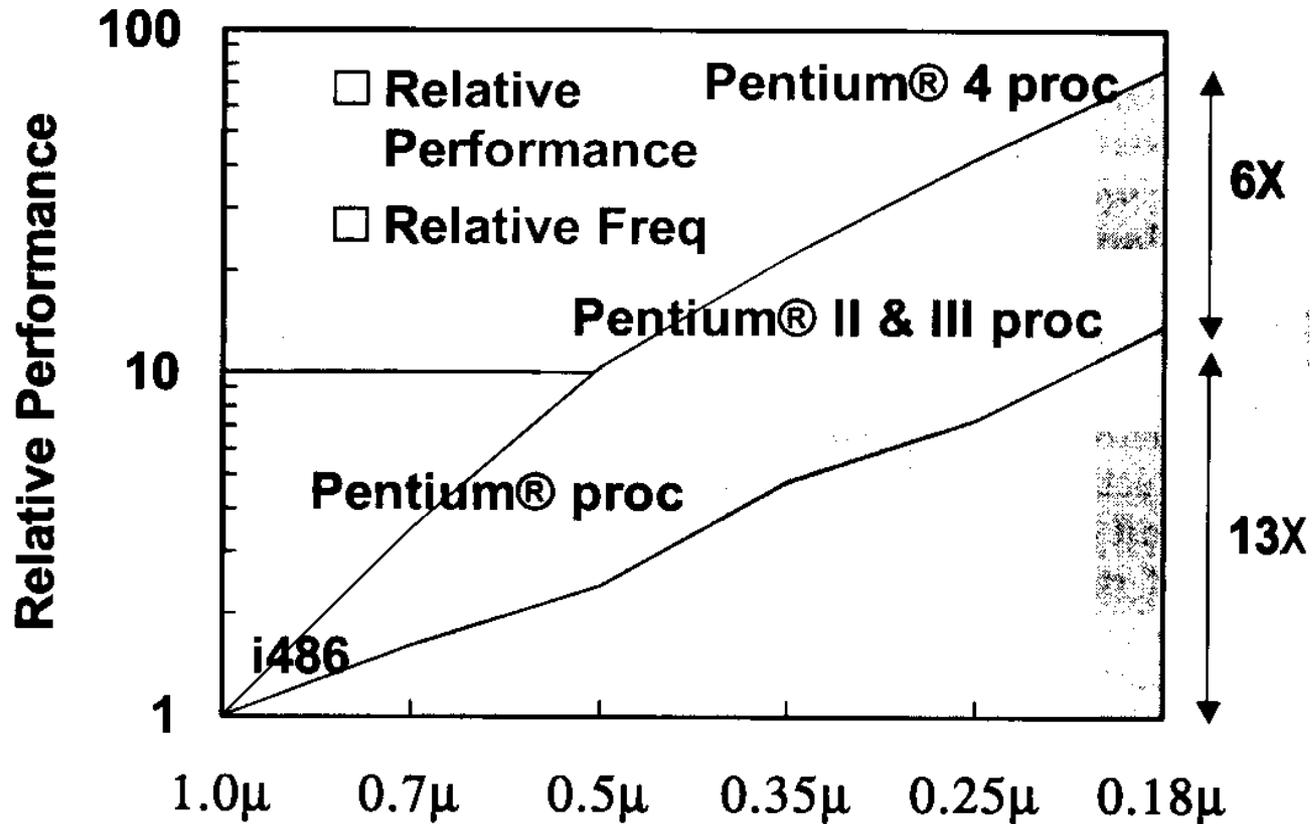
P.Gelsinger: μ Processors for the New Millenium, ISSCC 2001

μ Processor Power



P.Gelsinger: μ Processors for the New Millenium, ISSCC 2001

μ Processor Performance



2010 Outlook

- Performance 2X/16 months
 - 1 TIP (terra instructions/s)
 - 30 GHz clock
- Size
 - No of transistors: 2 Billion
 - Die: 40*40 mm
- Power
 - 10kW!!
 - Leakage: 1/3 active Power

Some interesting questions

- What will cause this model to break?
- When will it break?
- Will the model gradually slow down?
 - Power and power density
 - Leakage
 - Process Variation